TypeDB Fundamentals Lecture 4 17th January 2024

The Polymorphic Data Model With Types



Dr. Christoph Dorn

Head of Research, Vaticle

Previously: Theoretical Computer Scientist in Category Theory @ Oxford University



Prologue: The bigger picture

A brief overview of our Fundamentals Lecture Series



Lecture #1: The theoretical motivation

- Databases lack behind in providing *high-level "zero-cost" abstractions* as now found in many modern programming languages
- Type systems force developers to "think before they write", making applications not only more robust, but also more composable and maintainable
- With type theory succeeding predicate logic, "types as queries" is an ideal modern querying paradigm
- ... and it provides a framework for *polymorphism*

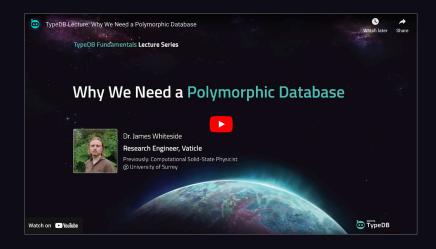


Watch at TypeDB.com/lectures



Lecture #2: The pragmatic pain points

- Regular mismatches between aged (or domain-specific) data modeling paradigms and modern programming language paradigms
 - Object-relational mismatch
 - Object-graph mismatch
 - Object-document mismatch
- Data Integrity, lack of Polymorphic Querying...
- Wrappers, like ORMs, often yield costly abstractions (non-optimal queries, additional object representations)



Watch at TypeDB.com/lectures



Lecture #3: The polymorphic database

- TypeDB builds directly on a novel *polymorphic* data model, equipped with type system that enables:
 - an expressive query language that can leverage inheritance and interface polymorphism
 - principled database engineering, which is maintainable and robust by design
 - complex applications that are modular and composable, continuously modifiable

TypeDB Lacture:
TypeDB Fundamentals Lecture Series

Share

TypeDB Fundamentals Lecture Series

Comparison of the polymorphic Database

TypeDB Fundamentals Lecture Series

Dr James Whiteside

Research Engineer, Vaticle

Previously:

Computational Solid-State Physicist

(Diniversity of Surrey)

Water Previously:

Water Previously:

Watch at TypeDB.com/lectures

Today's lecture: a deep dive into TypeDB's data model!



Lecture #4 overview

- Key modeling terminology: *concepts*, *instances*, *dependencies*
- Polymorphic entity-relation-attribute (PERA) model via TypeQL
- Comparison of PERA to other data model
- Pattern-based querying and reasoning



Part I: Concepts and instances

Illustrated guide to key terminology in conceptual modeling

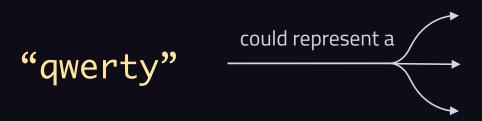


"qwerty"

Literal value

Data defined in an abstract mathematical framework

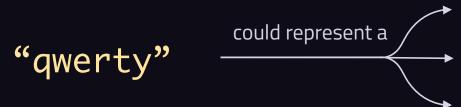




Literal value

Data defined in an abstract mathematical framework Plain-text password of a userMessage between Ana and BobKeyboard layout in our system





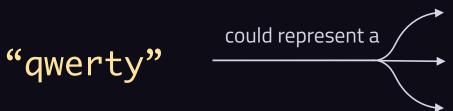
Literal value

Data defined in an abstract mathematical framework Plain-text password of a user
Message between Ana and Bob
Keyboard layout in our system

Concept

Meaningful categorization of data in the modeler's framework





Literal value

Data defined in an abstract mathematical framework Plain-text password of a user
Message between Ana and Bob
Keyboard layout in our system

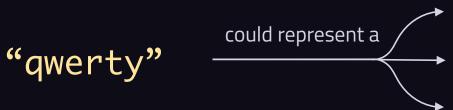
Concept

Meaningful categorization of data in the modeler's framework

Definition. *Concept formation* is the process of sorting data *or* data structures into meaningful classes a.k.a. *types*.

-Hunt, Earl B.. "concept formation". Encyclopedia Britannica





Literal value

Data defined in an abstract mathematical framework Plain-text password of a user
Message between Ana and Bob
Keyboard layout in our system

Concept

Meaningful categorization of data in the modeler's framework

Definition. *Concept formation* is the process of sorting data *or* data structures into meaningful classes a.k.a. *types*.

---Hunt, Earl B.. "concept formation". Encyclopedia Britannica







Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

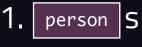




Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

Have concepts (i.e. types) of:







Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

Have concepts (i.e. types) of:

birthday S





Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

Have concepts (i.e. types) of: 1. person s

2.

- name s ----- instances are *strings*
- 3. birthday S ----- instances are *dates*





Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

Have concepts (i.e. types) of: 1. person s 2. name s → instances are strings 3. birthday s → instances are dates

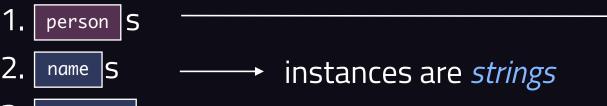




Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990

Have concepts (i.e. types) of:



3. birthday $s \longrightarrow$ instances are *dates*





Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990
"Bob"	01-Feb-1990

Have concepts (i.e. types) of:
1. person S
2. name S → instances are strings
3. birthday S → instances are dates





Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990
"Bob"	01-Feb-1990
NULL	NULL

Have concepts (i.e. types) of: 1. person s 2. name s → instances are strings 3. birthday s → instances are dates Are persons the sum of names and birthdays? ← No.

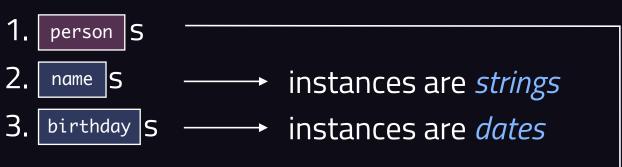




Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990
"Bob"	01-Feb-1990
NULL	NULL

Have concepts (i.e. types) of:







Tables are a *specific* example... Definitions apply to data models in general as we will later see!

person	
name	birthday
"Ana"	31-May-1997
"Bob"	01-Feb-1990
"Bob"	01-Feb-1990
NULL	NULL

Have concepts (i.e. types) of: 1. person s 2. name s → instances are strings 3. birthday s → instances are dates

Are persons the sum of names and birthdays? - No. Instances of person are rows!

Definition. Two kinds of types:

- 1. Those collecting *literal values*
- 2. Those collecting *freely constructible objects*

→ attribute types

→ object types



person	
name	birthday
"Ana"	NULL
NULL	01-Feb-1990



person	
name	birthday
"Ana"	NULL
NULL "Bob"	01-Feb-1990



person						
name birthday						
"Ana"	NULL					
NULL "Bob"	01-Feb-1990					

creating **new name** *requires* a person instance (i.e. row) to "*have* that name"



person					
name	birthday				
"Ana"	NULL				
NULL "Bob"	01-Feb-1990				

creating **new name** *requires* a person instance (i.e. row) to "*have* that name"

employee					
emp_id	name				
1	"Ana"				
2	"Bob"				

team					
team_id	team_name				
1	"Engineering"				
2	"Marketing"				

team_membership					
employee	team				
1	1				
2	1				





person					
name	birthday				
"Ana"	NULL				
NULL "Bob"	01-Feb-1990				

creating **new name** *requires* a **person** instance (i.e. row) to "*have* that name"

emp	employee		team			team_memb	ership
emp_id	name		team_id	team_name		employee	team
1	"Ana"		1	"Engineering"	_	1	1
2	"Bob"		2	"Marketing"	\mathcal{C}	2	1

creating new team_membership requires an employee and a team



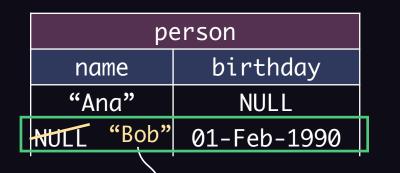
person							
name	birthday						
"Ana"	NULL						
NULL "Bob"	01-Feb-1990						

creating **new name** *requires* a **person** instance (i.e. row) to "*have* that name"

emp	employee		team			team_memb	ership
emp_id	name		team_id	team_name		employee	team
1	"Ana"	_ [1	"Engineering"		1	1
2	"Bob"		2	"Marketing"	\sim	2	1

creating new team_membership requires an employee and a team





Definition. A concept *depends* on another concept if instantiating the former requires references to instances of the latter.

creating **new name** *requires* a **person** instance (i.e. row) to "*have* that name"

emp	mployee		team			team_memb	ership
emp_id	name		team_id	team_name	_	employee	team
1	"Ana"		1	"Engineering"		1	1
2	"Bob"		2	"Marketing"	\sim	2	1

creating new team_membership requires an employee and a team



person							
name	birthday						
"Ana"	NULL						
NULL "Bob"	01-Feb-1990						

creating **new name** *requires* a **person** instance (i.e. row) to "*have* that name"

Definition. A concept *depends* on another concept if instantiating the former requires references to instances of the latter.

emp	employee		team			team_memb	ership
emp_id	name	_	team_id	team_name		employee	team
1	"Ana"	. [1	"Engineering"		1	1
2	"Bob"		2	"Marketing"		2	1
							FKa

creating new team_membership requires an employee and a team



	emplo	oyee			team
	emp_id	name		team_id	team_name
11	1	"Ana"		1	"Engineering"
Schema	2	"Bob"		2	"Marketing"
he				·	
Sci		team_me	mŁ	pership	

team_membership				
employee team				
1	1			
2	1			

employee

1

2

emplo	employee		team		
emp_id	name	team_id	team_name		
1	"Ana"	1	"Engineering"		
2	"Bob"	2	"Marketing"		
·					
	team_men	nbership			

team

1

1

Schema 1

\sim	
D	
L	
<i>a</i>	
Ch	
S	

employee				
emp_id name				
1	"Ana"			
2	"Bob"			

team	1
team_name	employees
"Engineering"	[1,2]
"Marketing"	[]

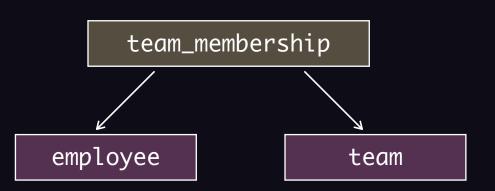


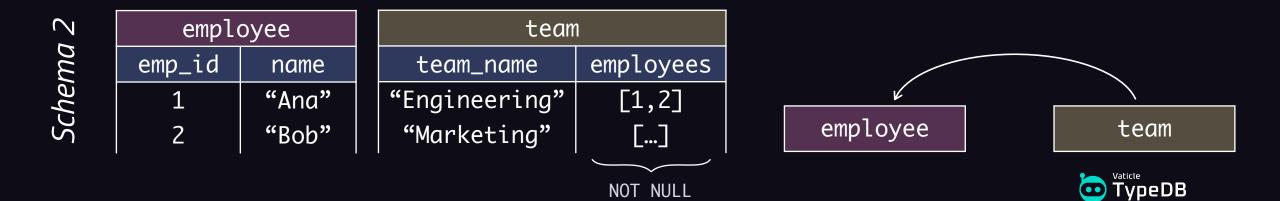
7

Schema

emplo	oyee		team
emp_id	name	team_id	team_name
1	"Ana"	1	"Engineering"
2	"Bob"	2	"Marketing"
[team_mem	bership	
	employee	team	
	1	1	
	2	1	

Dependency hierarchy





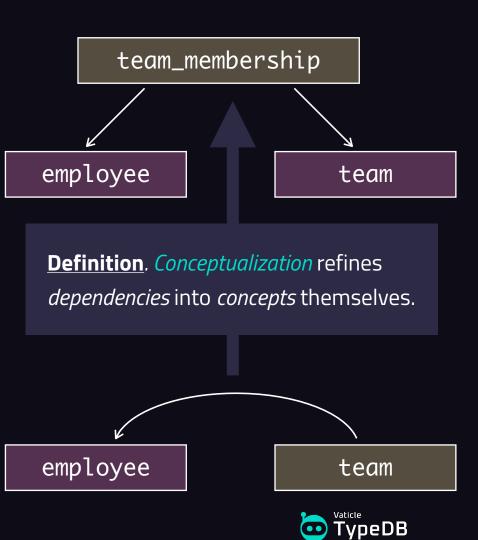
7

Schema

Schema 2

employee		team		
emp_id	name	team_id	team_id tea	
1	"Ana"	1	"Eng	ineering"
2	"Bob"	2	"Ma	rketing"
	team_mem	bership		
	employee	team		
	1	1		
2		1		
empl	oyee		tean	1
emp_id name		team_r	team_name	
1	"Ana"	"Enginee	"Engineering"	
2	"Bob"	"Market	ing"	[]

Dependency hierarchy



NOT NULL

7

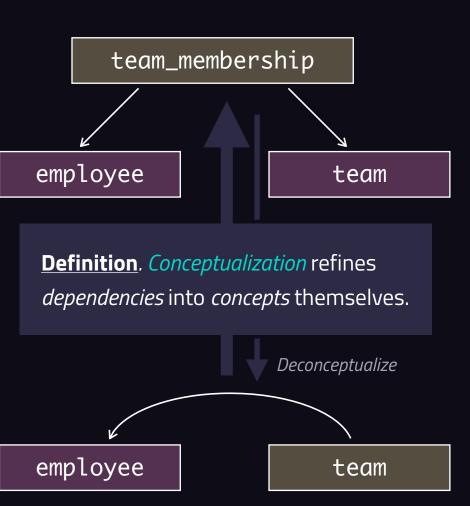
Schema

Schema 2

employee			team			
emp_id	name		team_id	te	team_name	
1	"Ana"		1	"Eng	ineering"	
2	"Bob"		2	"Marketing"		
team_men		mŁ	pership			
	employee	j	team			
	1		1			
	2		1			
employee			team			
emp_id	name		team_name		employees	
1	"Ana"		"Engineering"		[1,2]	
2	"Bob"		"Marketing"		[]	

NOT NULL

Dependency hierarchy





TypeDB

Concept formation sorts our data into meaningful types

person	person	
	name	birthday
name	"Ana"	31-May-1997
	"Bob"	01-Feb-1990
birthday	"Bob"	01-Feb-1990



Concept formation sorts our data into meaningful types

Some types can be freely instantiated (objects types),
 Others collect pre-defined values (attribute types)

person		person	
		name	birthday
name		"Ana"	31-May-1997
	_	"Bob"	01-Feb-1990
oirthday		"Bob"	01-Feb-1990



Concept formation sorts our data into meaningful types

model allows us to

"invent" new instances!

 Some types can be freely instantiated (objects types), Others collect pre-defined values (attribute types)

erson	person	
	name	birthday
name	"Ana"	31-May-1997
	"Bob"	01-Feb-1990
rthday	"Bob"	01-Feb-1990

bi

"Bob" 01-Feb-1990



- Concept formation sorts our data into meaningful types
- Some types can be freely instantiated (objects types),
 Others collect pre-defined values (attribute types)

cannot invent new instances!
 value creation is idempotent

model allows us to

"invent" new instances!

erson	person	
	name	birthday
name	"Ana"	31-May-1997
	"Bob"	01-Feb-1990
rthday	"Bob"	01-Feb-1990

"Bob" | 01-Feb-1990

"Bob"

bi



- *Concept formation* sorts our data into meaningful *types*
- Some types can be freely instantiated (objects types),
 Others collect pre-defined values (attribute types)

→ cannot invent new instances! value creation is idempotent

model allows us to

"invent" new instances!

 Dependencies indicate instantiation of types must reference instances of other types

person		person	
		name	birthday
name		"Ana"	31-May-1997
	-	"Bob"	01-Feb-1990
irthday		"Bob"	01-Feb-1990

"Bob" | 01-Feb-1990

"Bob"



- *Concept formation* sorts our data into meaningful *types*
- Some types can be freely instantiated (objects types), Others collect pre-defined values (attribute types)

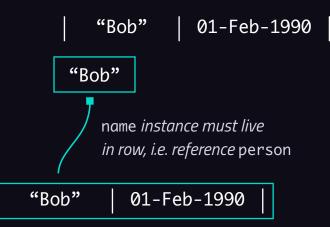
→ cannot invent new instances! value creation is idempotent

model allows us to

"invent" new instances!

 Dependencies indicate instantiation of types must reference instances of other types

person		person	
		name	birthday
name		"Ana"	31-May-1997
	_	"Bob"	01-Feb-1990
irthday		"Bob"	01-Feb-1990





- Concept formation sorts our data into meaningful types
- Some types can be freely instantiated (objects types), Others collect pre-defined values (attribute types)

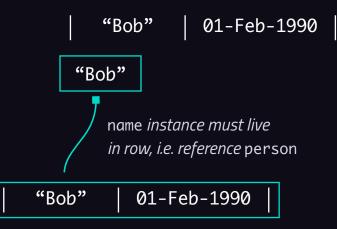
→ cannot invent new instances! value creation is idempotent

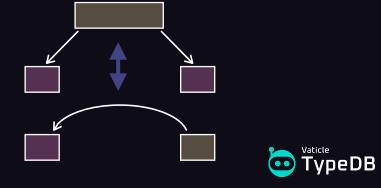
model allows us to

"invent" new instances!

- Dependencies indicate instantiation of types must reference instances of other types
- *Conceptualization* turns a dependency into a concept itself

name birthday	/
name "Ana" 31-May-19	97
"Bob" 01-Feb-19	90
rthday "Bob" 01-Feb-19	90





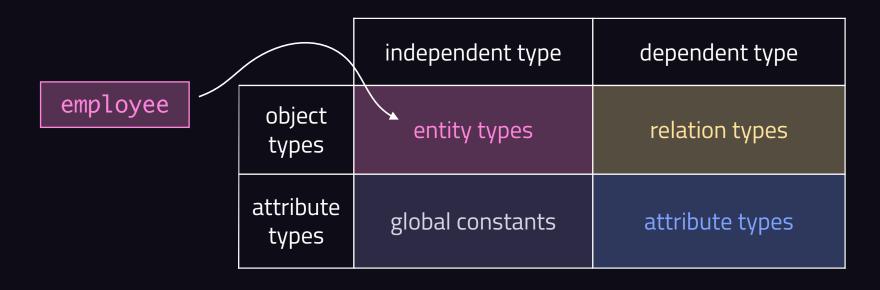
Part II: The polymorphic data model

Exploring the PERA model with TypeQL

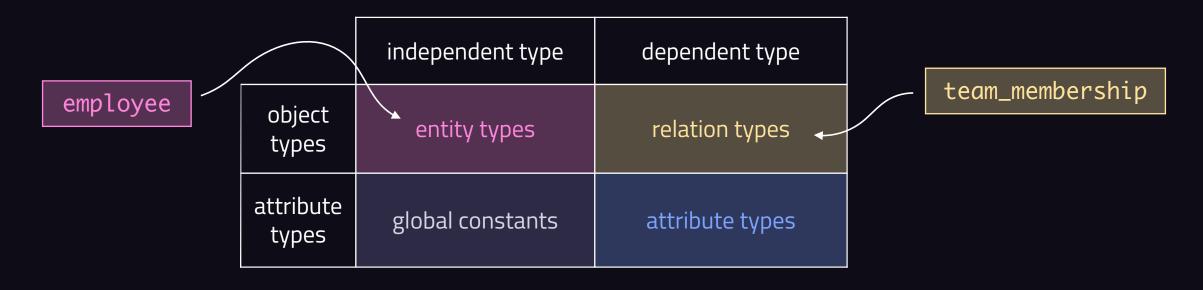


	independent type	dependent type
object types	entity types	relation types
attribute types	global constants	attribute types

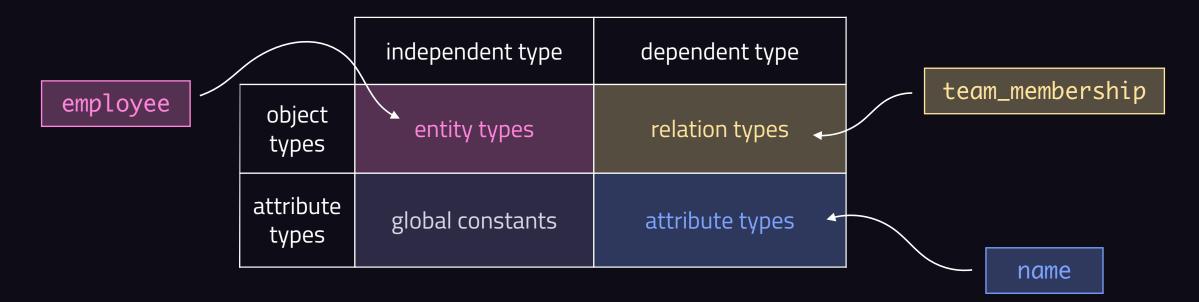






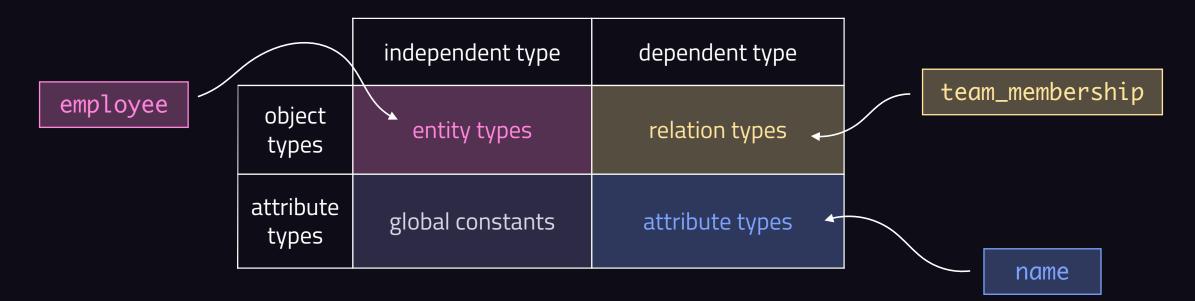








 The polymorphic entity-relation-attribute (PERA) builds directly on our previous definitions of types, instances, dependencies in conceptual modeling, with key kinds of types:



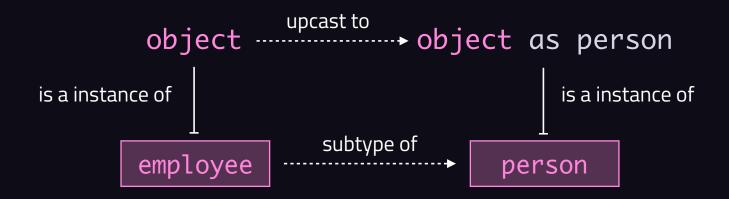
 Incidentally, the above 2 x 2 classification closely matches classical ERA modeling, however, for us, it fundamentally derives from simple type-theoretic principles.



- Type system defines *types* and *type operations* to pass between types
- A fundamental operation is *subtyping*, allowing to cast type instances:

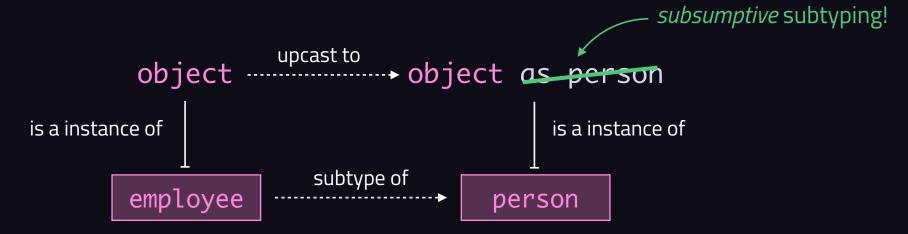


- Type system defines *types* and *type operations* to pass between types
- A fundamental operation is *subtyping*, allowing to cast type instances:



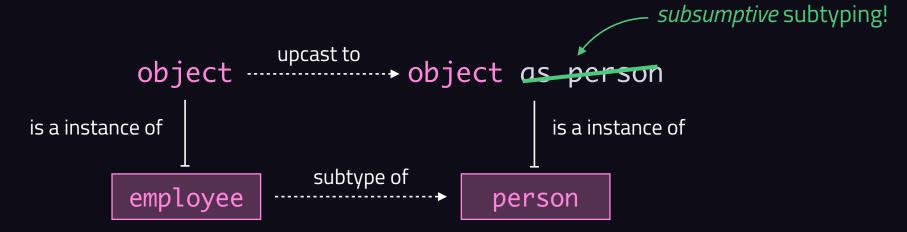


- Type system defines *types* and *type operations* to pass between types
- A fundamental operation is *subtyping*, allowing to cast type instances:



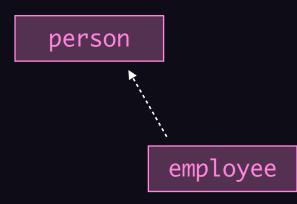


- Type system defines *types* and *type operations* to pass between types
- A fundamental operation is *subtyping*, allowing to cast type instances:

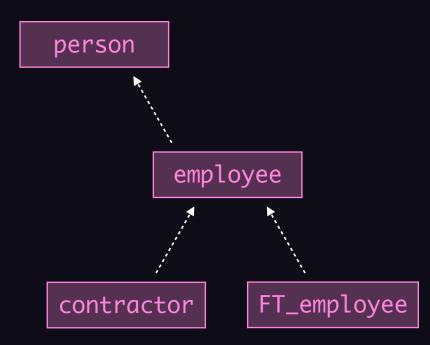


A name "Ana" in type name can be cast into the bare string "Ana" in type string

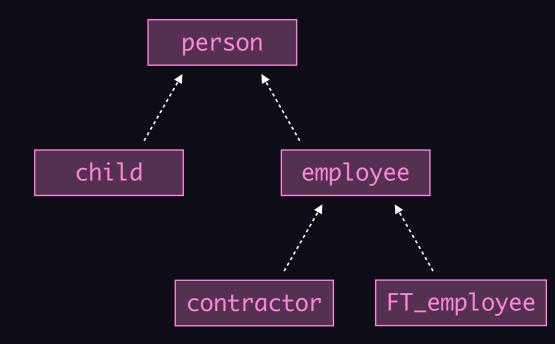




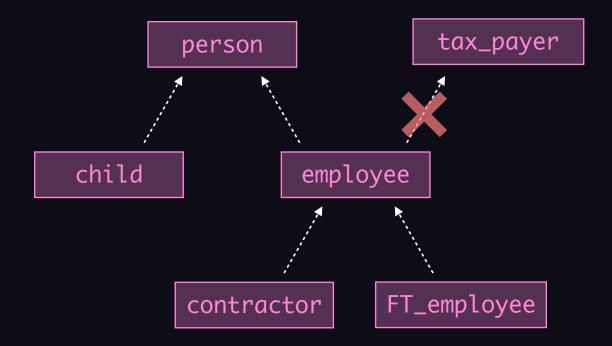






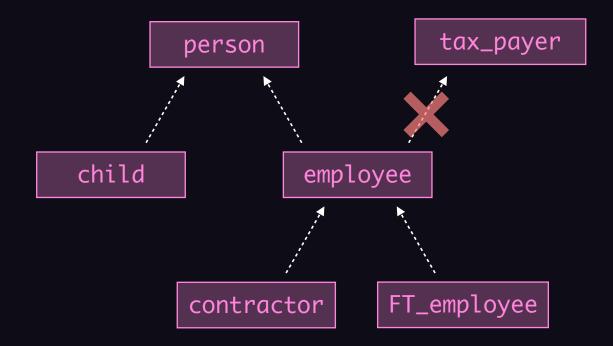








• The PERA model supports *inheritance type hierarchies* to describe concept specialization

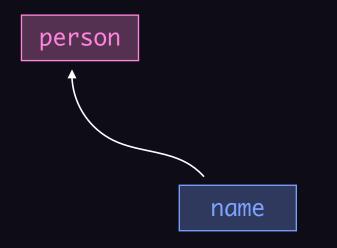


<u>**Condition</u>**: the PERA model enforces *single inheritance*, meaning types may have at most one parent type.</u>

- avoids the "diamond problem"
- enforces more performant model design

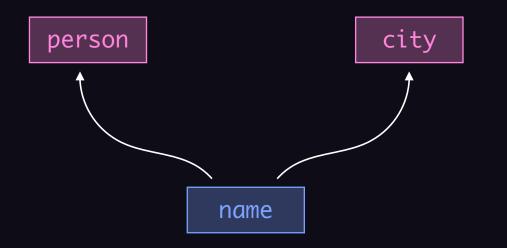


• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*



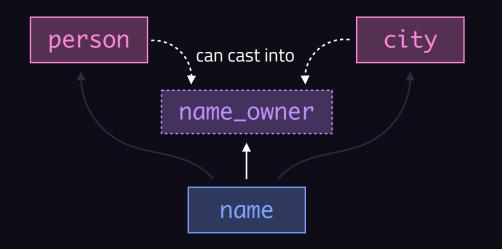


• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*





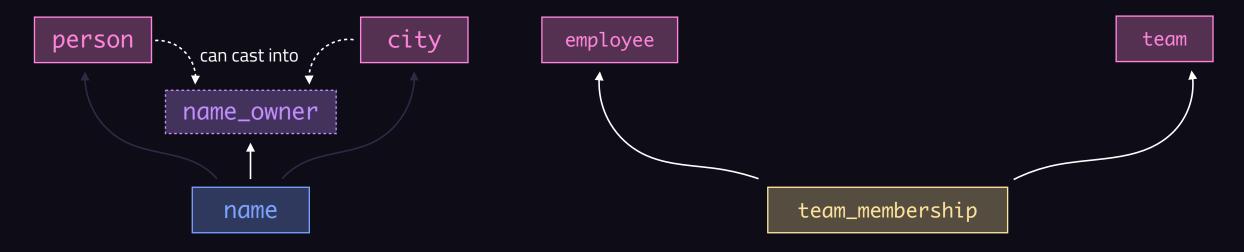
• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*



"cities, like persons, have the capability to be name owners"



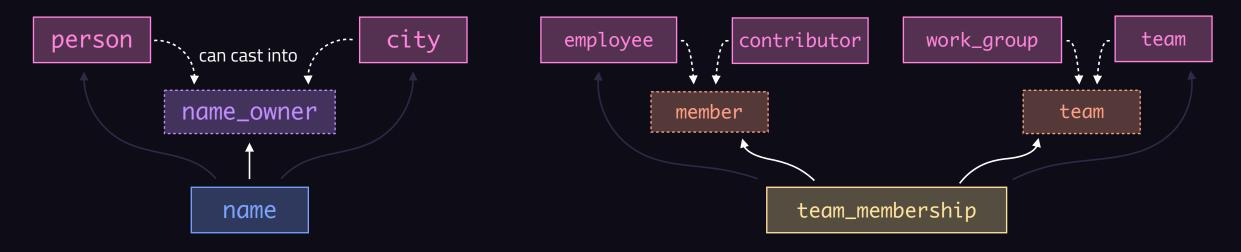
• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*



"cities, like persons, have the capability to be name owners"



• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*

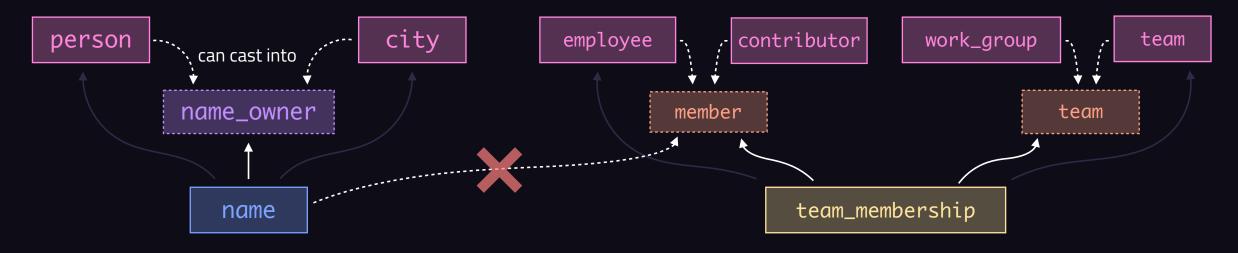


"cities, like persons, have the capability to be name owners"

"contributors, like employees, have the capability to be team members"



• The PERA model *abstracts type dependencies* as *type capabilities implementable by other types*



"cities, like persons, have the capability to be name owners"

"contributors, like employees, have the capability to be team members"

<u>Condition</u>: the PERA model enforces that *only object types* can be given capabilities. *Object types may implement many interfaces!*

- ----- avoids ambiguity due to idempotent value creation
- \longrightarrow c.f. "single-inheritance"



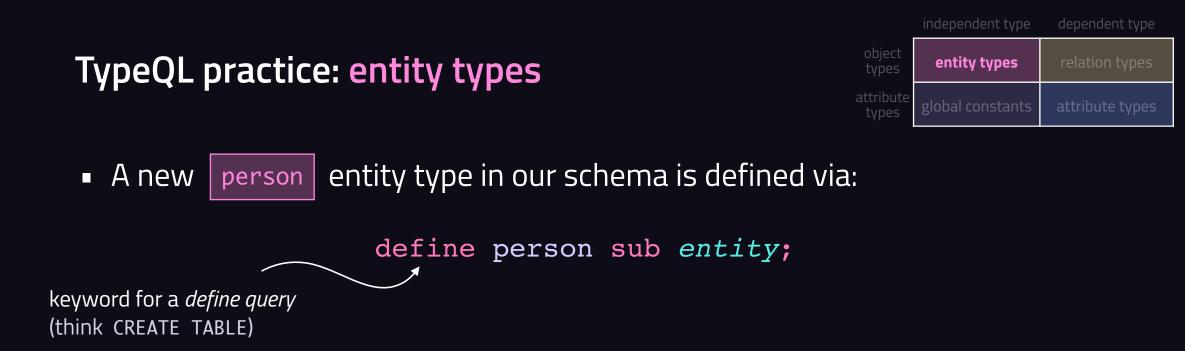
TypeQL practice: entity types

	independent type	dependent type	
object types	entity types	relation types	
attribute types	global constants	attribute types	

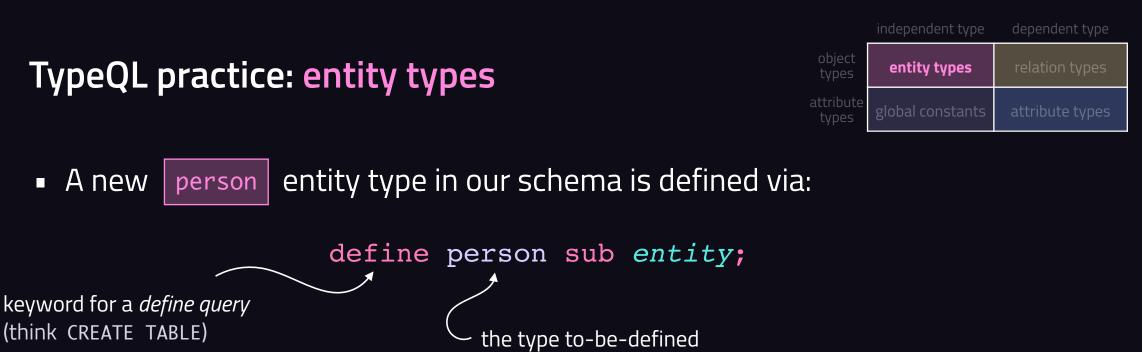
• A new person entity type in our schema is defined via:

define person sub entity;

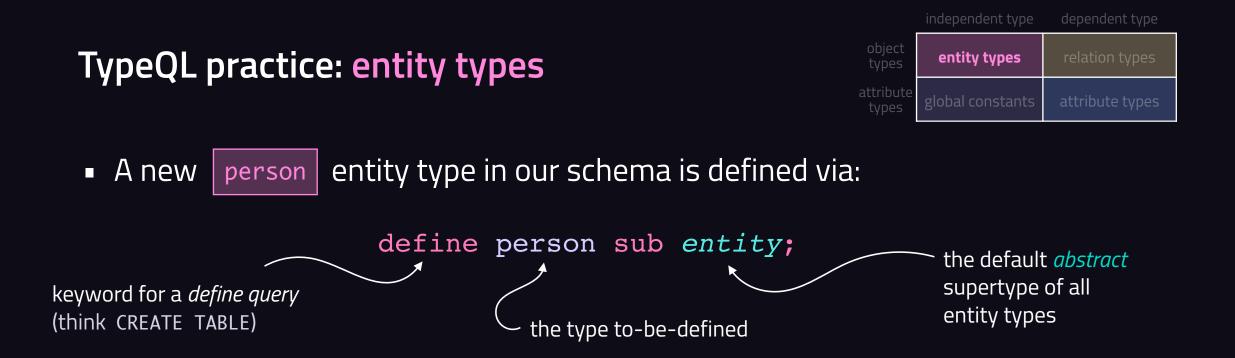




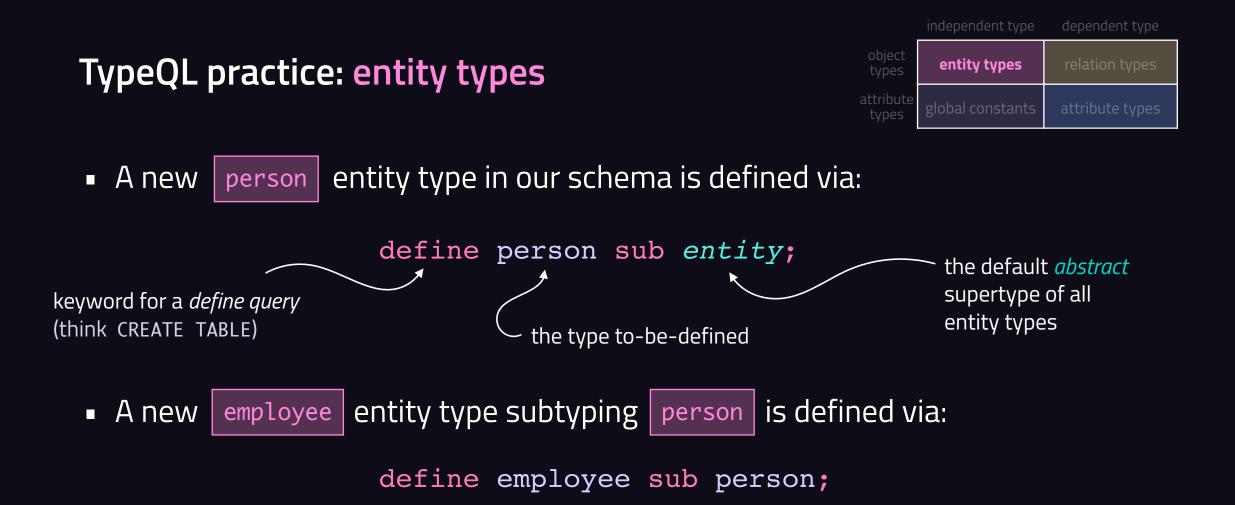




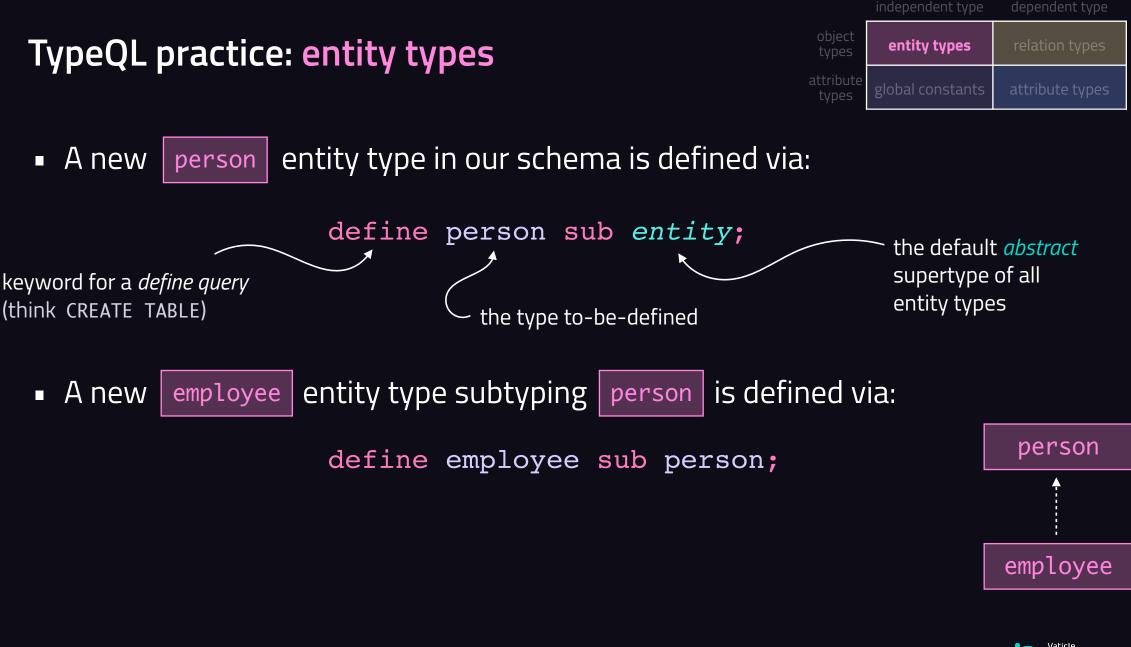


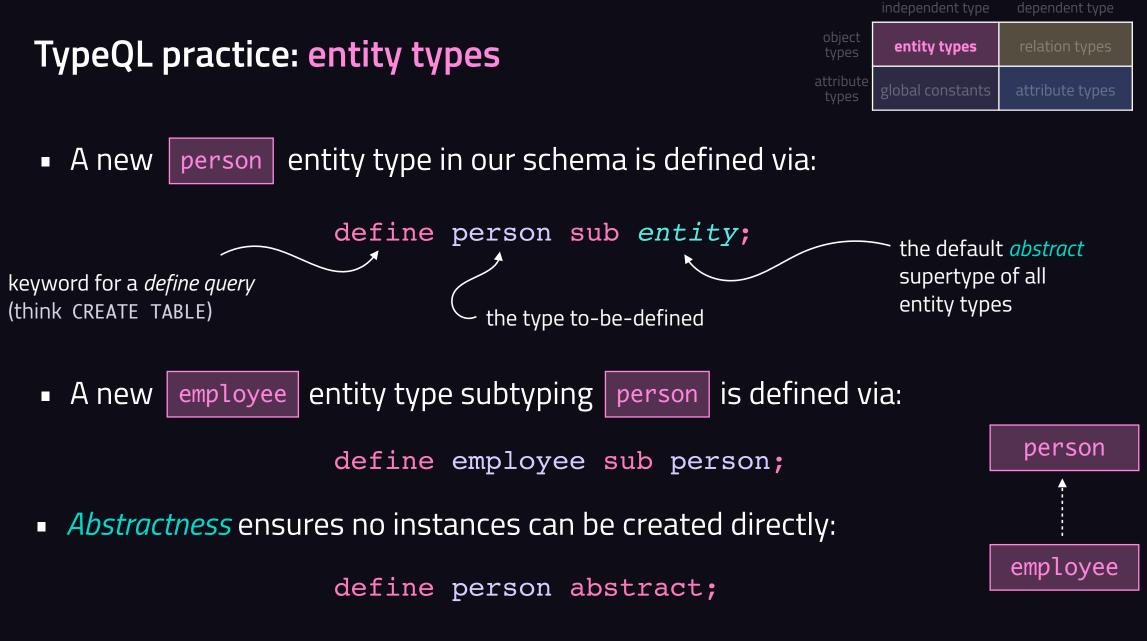




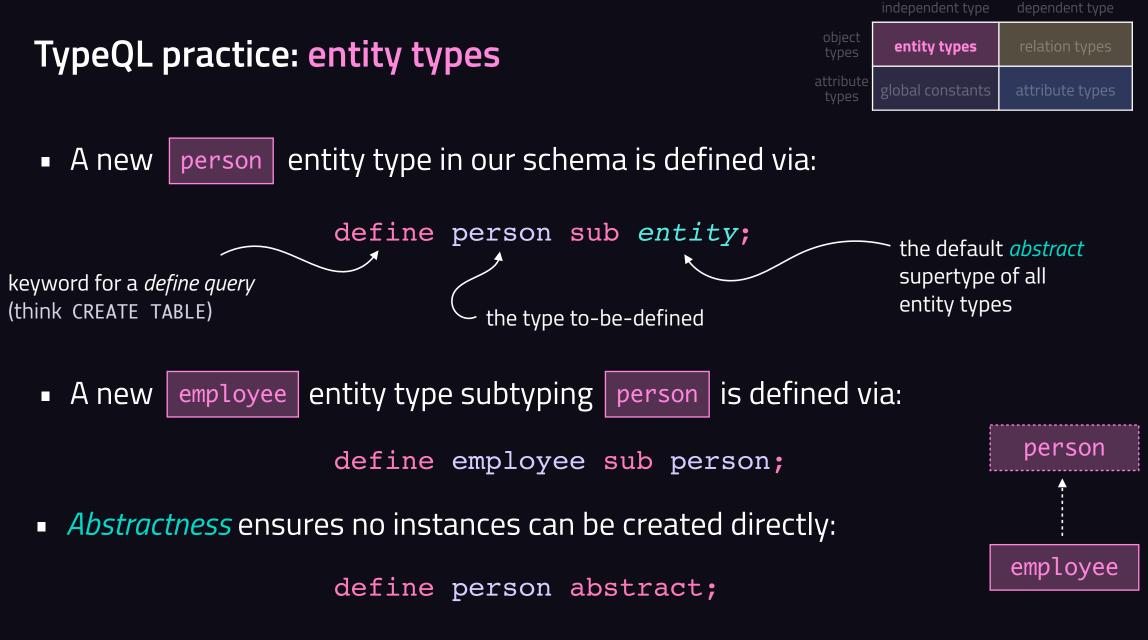














	independent type	dependent type
object types	entity types	relation types
ttribute types	global constants	attribute types

Define new marriage relation type...

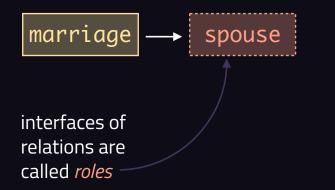
define
marriage sub relation,
 relates spouse;



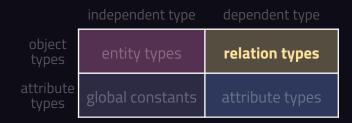
	independent type	dependent type
object types	entity types	relation types
ttribute types	global constants	attribute types

Define new marriage relation type...

```
define
marriage sub relation,
    relates spouse;
```





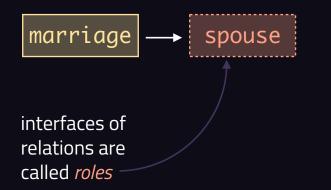


Define new marriage relation type...

define
marriage sub relation,
 relates spouse;

and several subtypes:

case 1: role overwriting
define
hetero_marriage sub marriage,
 relates husband as spouse,
 relates wife as spouse;





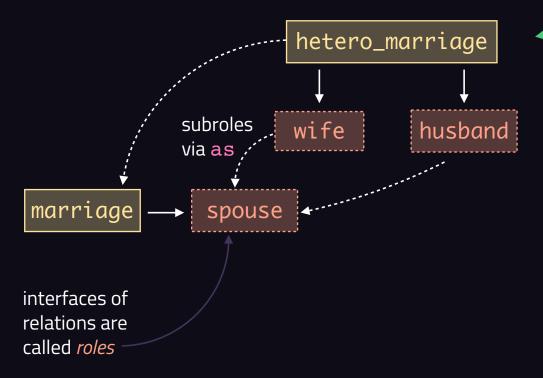


Define new marriage relation type...

define

marriage sub relation,

relates spouse;



and several subtypes:

case 1: role overwriting define hetero_marriage sub marriage, relates husband as spouse, relates wife as spouse;



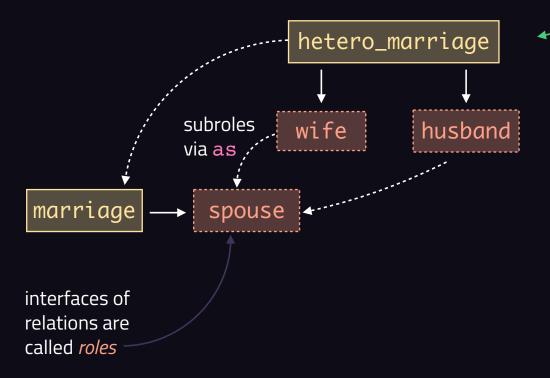


Define new marriage relation type...

define

marriage sub relation,

relates spouse;



and several subtypes:

case 1: role overwriting define hetero_marriage sub marriage, relates husband as spouse, relates wife as spouse;

case 2: role inheritance
define
religious_marriage sub marriage;



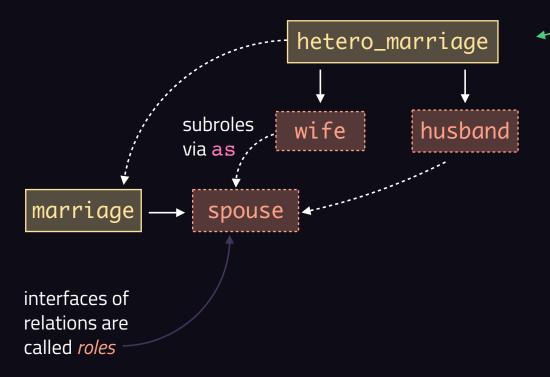


Define new marriage relation type...

define

marriage sub relation,

relates spouse;



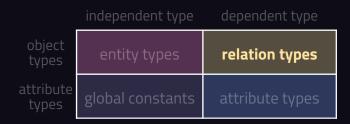
and several subtypes:

case 1: role overwriting define hetero_marriage sub marriage, relates husband as spouse, relates wife as spouse;

case 2: role inheritance
define
religious_marriage sub marriage;

case 3: role extension
define
witnessed_marriage sub marriage,
 relates witness;



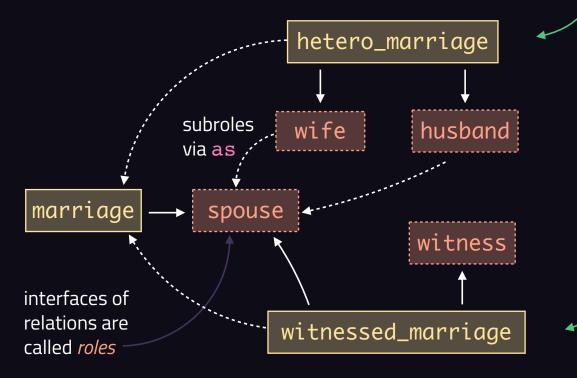


Define new marriage relation type...

define

marriage sub relation,

relates spouse;



and several subtypes:

case 1: role overwriting define hetero_marriage sub marriage, relates husband as spouse, relates wife as spouse;

case 2: role inheritance
define
religious_marriage sub marriage;

case 3: role extension define witnessed_marriage sub marriage, relates witness;



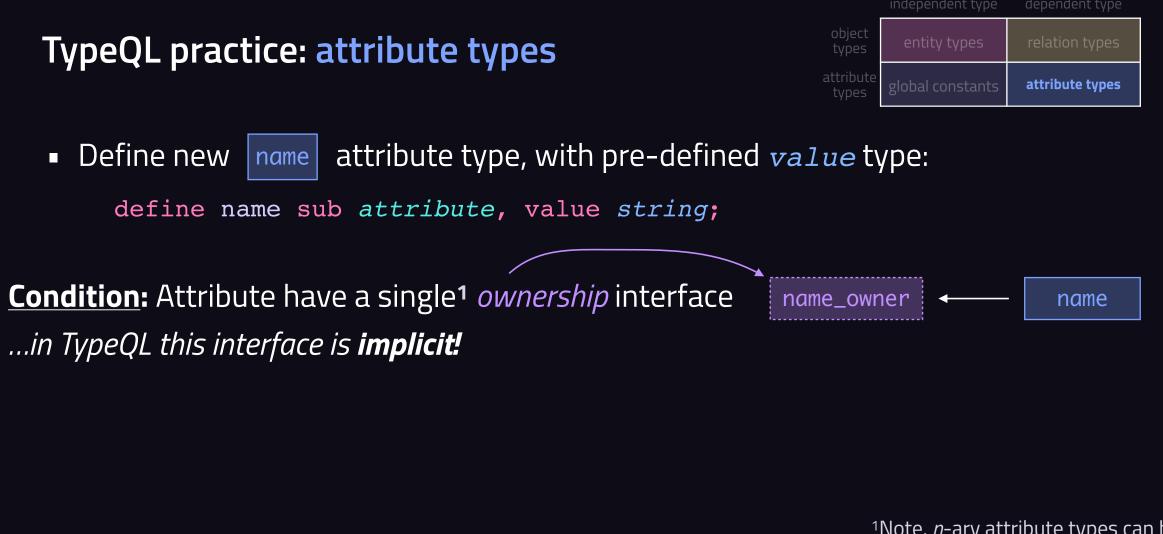
TypeQL practice: attribute types

	independent type	dependent type
object types	entity types	relation types
attribute types	global constants	attribute types

Define new name attribute type, with pre-defined value type:

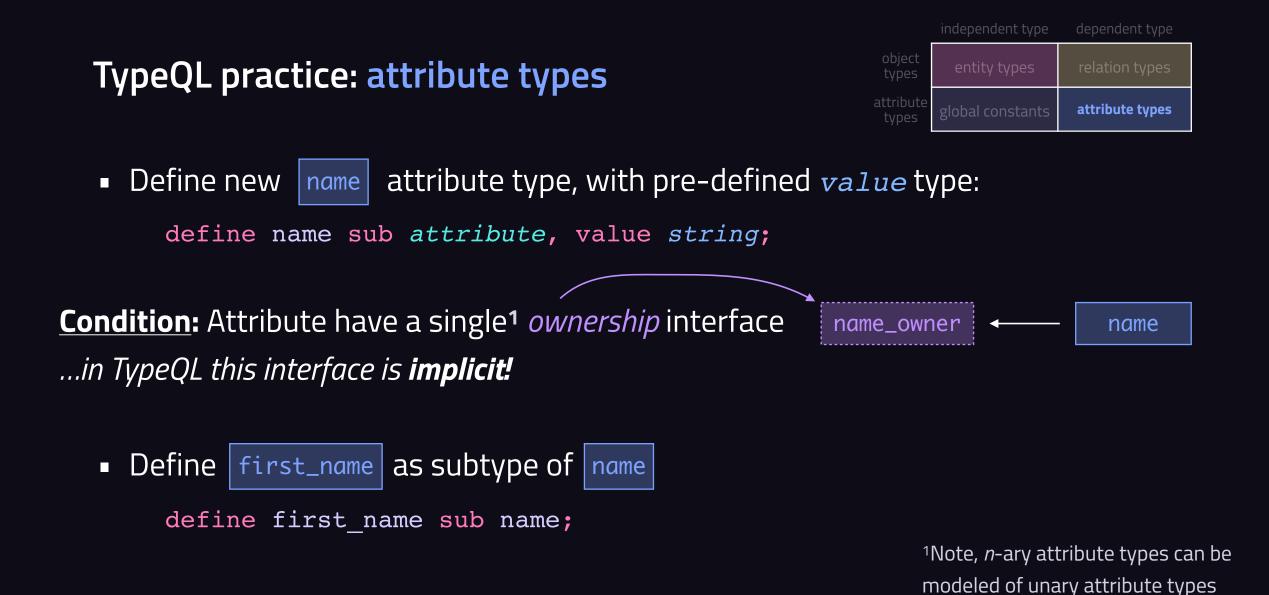
define name sub attribute, value string;



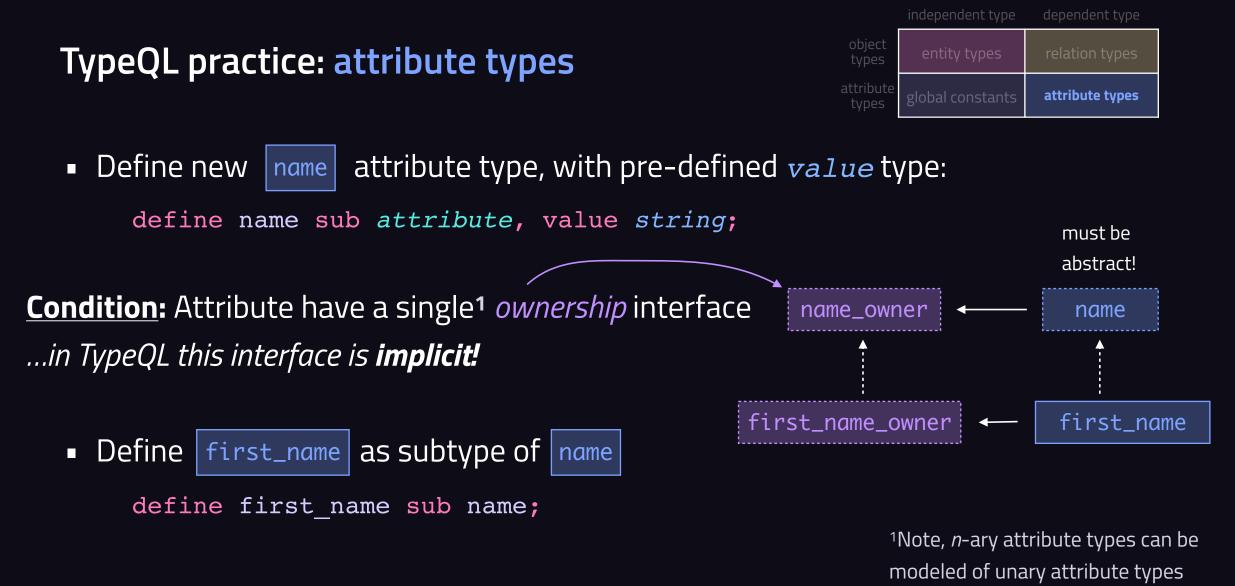


¹Note, *n*-ary attribute types can be modeled of unary attribute types of *n*-ary relation types



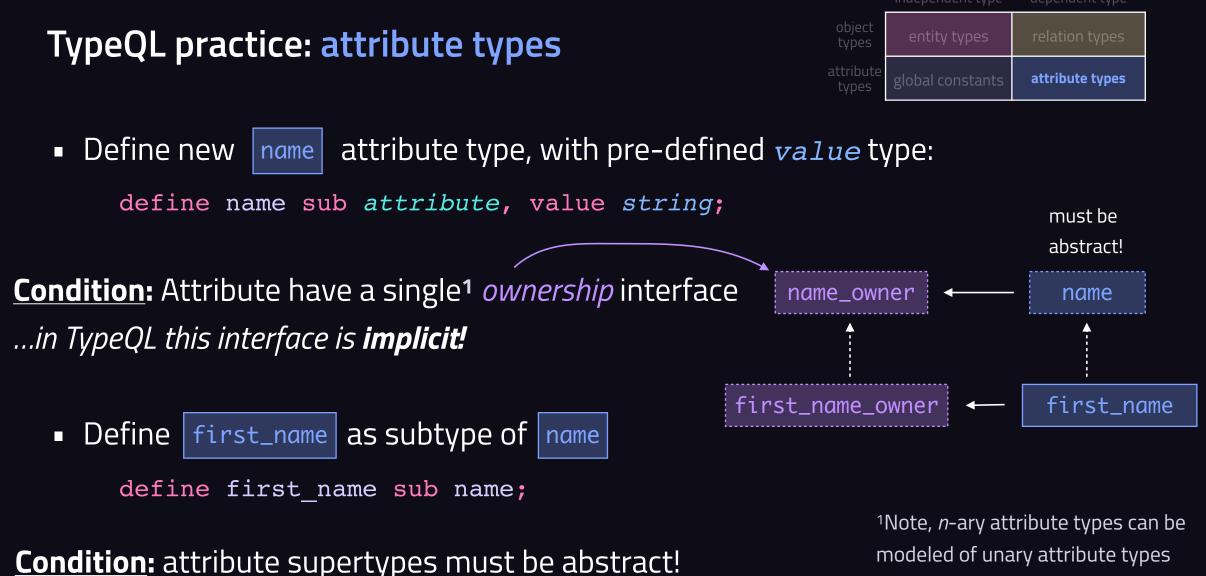


of *n*-ary relation types



of *n*-ary relation types





----- avoids ambiguity due to idempotent value creation

of *n*-ary relation types



• Object types can implement (i.e. "play") roles, defined via:

define person plays marriage:spouse;



Object types can implement (i.e. "play") roles, defined via:

define person plays marriage: spouse;

the scoped marriage: spouse is used here since role identifiers need only be unique *within* relation type hierarchies



• Object types can implement (i.e. "play") roles, defined via:

define person plays marriage: spouse;



the scoped marriage: spouse is used here since role identifiers need only be unique *within* relation type hierarchies

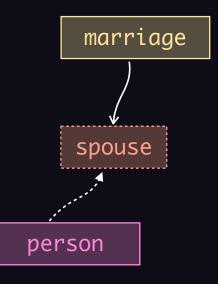


Object types can implement (i.e. "play") roles, defined via:

define person plays marriage: spouse;



the scoped marriage **:** spouse is used here since role identifiers need only be unique *within* relation type hierarchies





Object types can implement (i.e. "play") roles, defined via:

spouse

marriage

define person plays marriage: spouse;

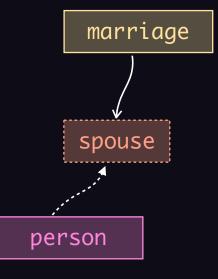
"persons can be

cast into spouses"

Role capabilities are *inherited*

person

define civil_servant sub person; registry_entry sub relation, relates registrar, relates event; civil_servant plays registry_entry:registrar; marriage plays registry_entry:event; the scoped marriage: spouse is used here since role identifiers need only be unique *within* relation type hierarchies





Object types can implement (i.e. "play") roles, defined via:

define person plays marriage: spouse; "persons can be marriage person spouse event cast into spouses marriage Role capabilities are *inherited* registry_entry define spouse civil servant sub person; registry entry sub relation, registrar relates registrar, person relates event; civil_servant plays registry_entry:registrar; marriage plays registry entry:event; civil_servant



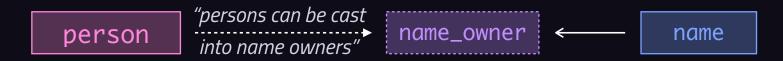
the scoped marriage: spouse is used here since role identifiers need only be unique *within* relation type hierarchies

- Object types can implement ownership of (i.e. "own") attribute types:
 - define person owns name;



• Object types can implement ownership of (i.e. "own") attribute types:

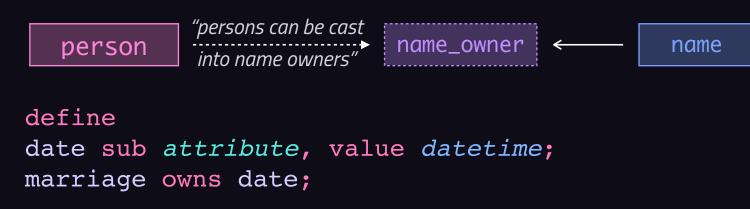
define person owns name;





• Object types can implement ownership of (i.e. "own") attribute types:

define person owns name;





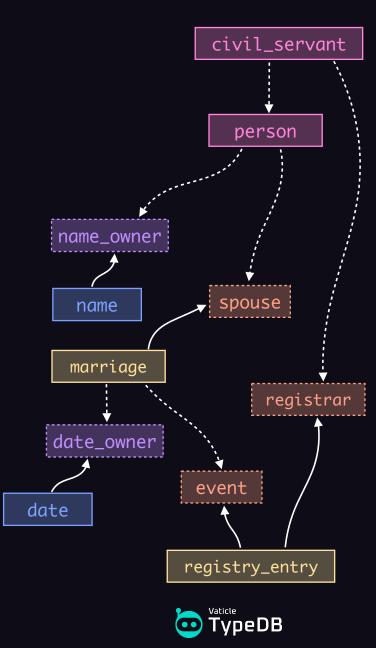


• Object types can implement ownership of (i.e. "own") attribute types:

• Like for roles, ownership capabilities are *inherited*

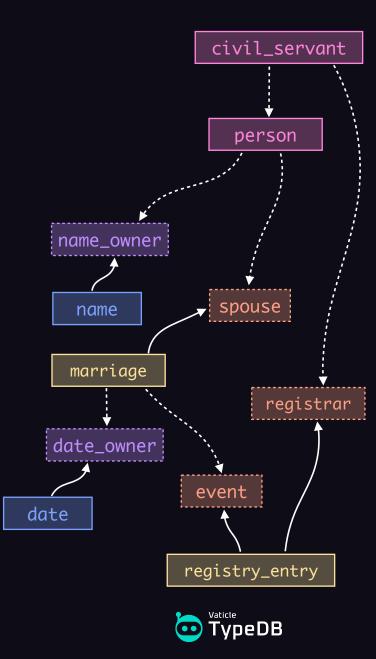


- For given type schema can
 insert data instances
- Must account for value types and dependencies



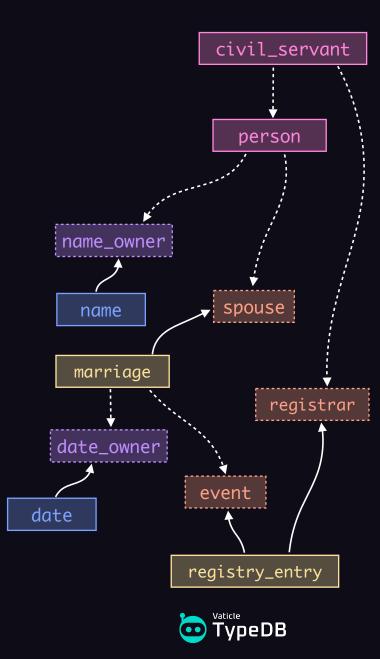
- For given type schema can
 insert data instances
- Must account for value types and dependencies

```
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



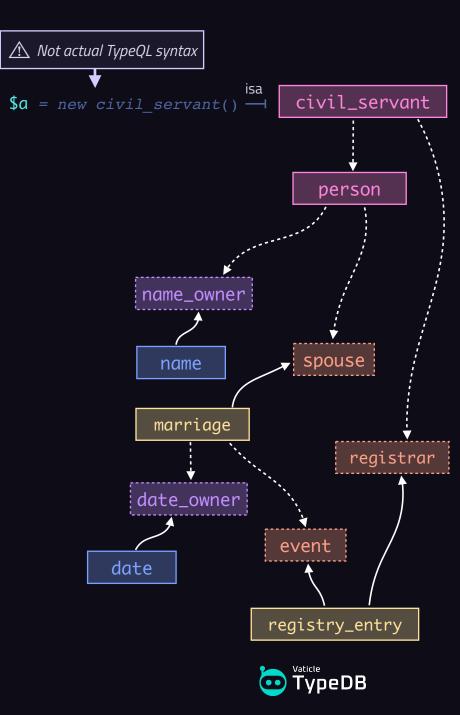
- For given type schema can
 insert data instances
- Must account for value types and dependencies

```
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



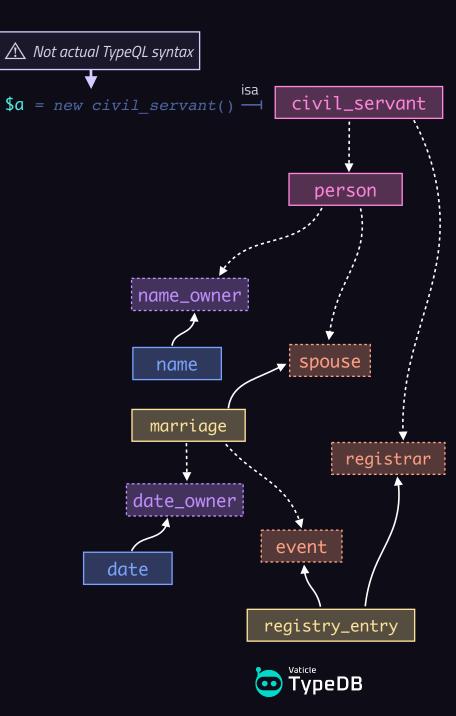
- For given type schema can insert data instances
- Must account for value types and dependencies

```
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
   has name "Bob";
$b2 isa person,
   has name "Bob";
$m (spouse: $b1, spouse: $b2)
   isa marriage,
   has date 17-05-2004;
(event: $m, registrar: $a)
   isa registry_entry;
```



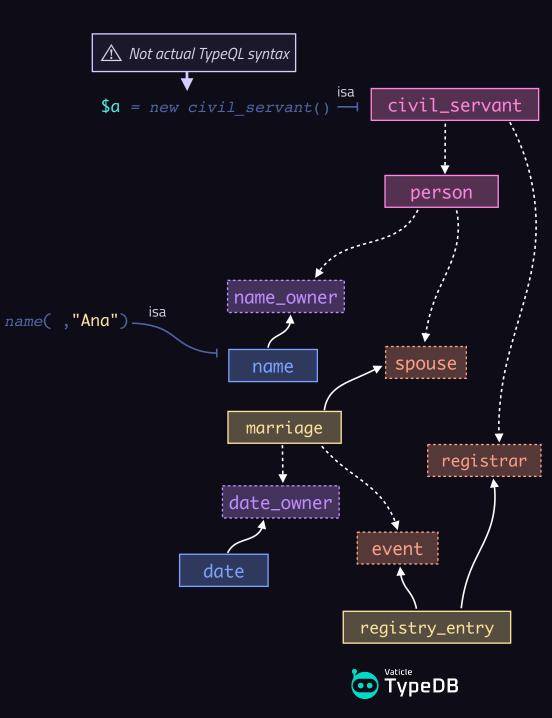
- For given type schema can insert data instances
- Must account for value types and dependencies

```
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2;
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



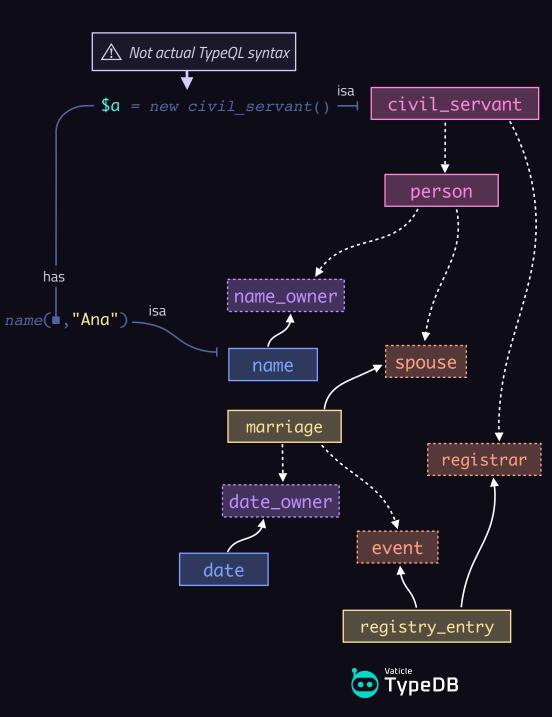
- For given type schema can
 insert data instances
- Must account for value types and dependencies

insert

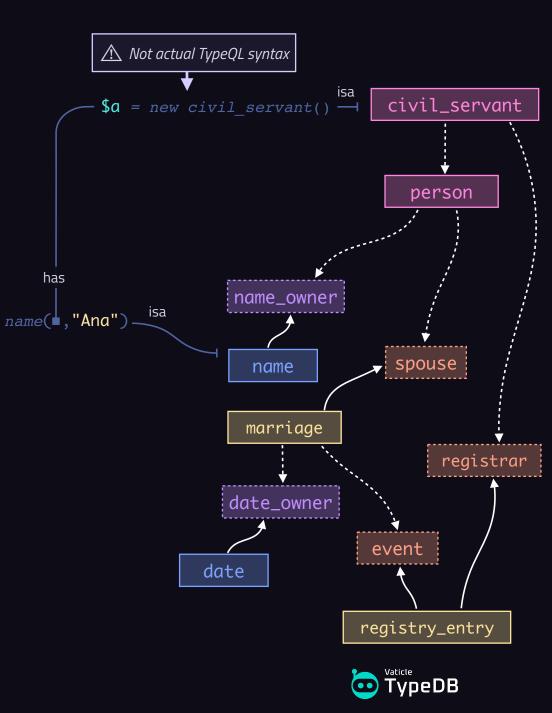


- For given type schema can insert data instances
- Must account for value types and dependencies

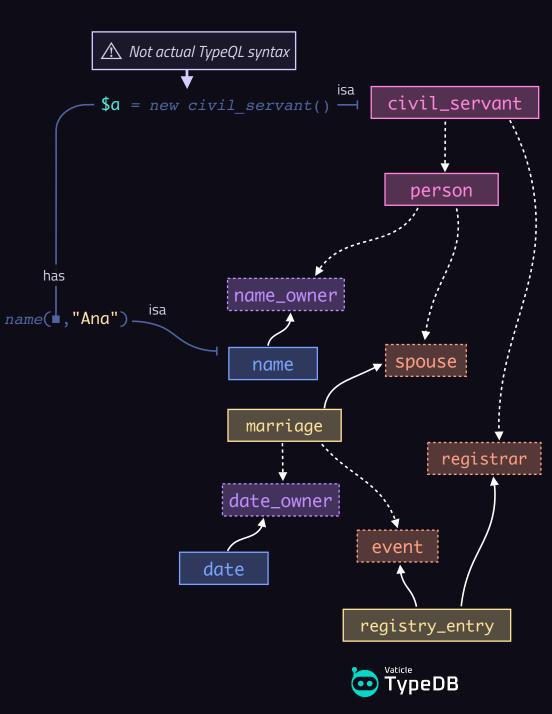
```
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



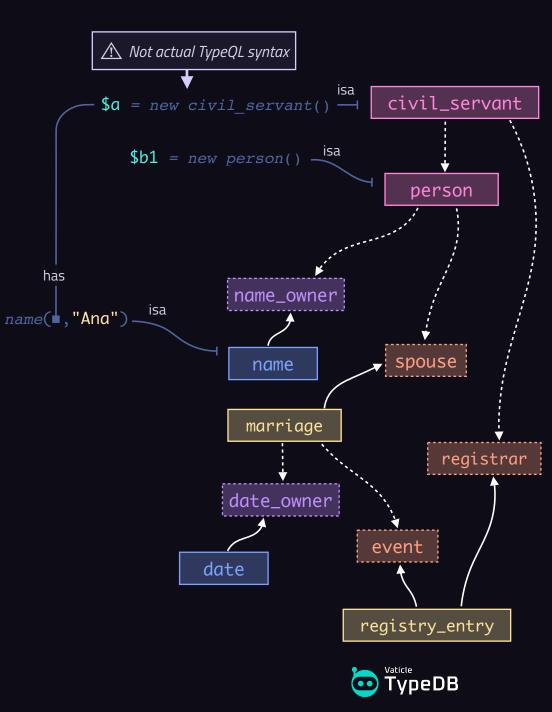
- For given type schema can insert data instances
- Must account for value types and dependencies



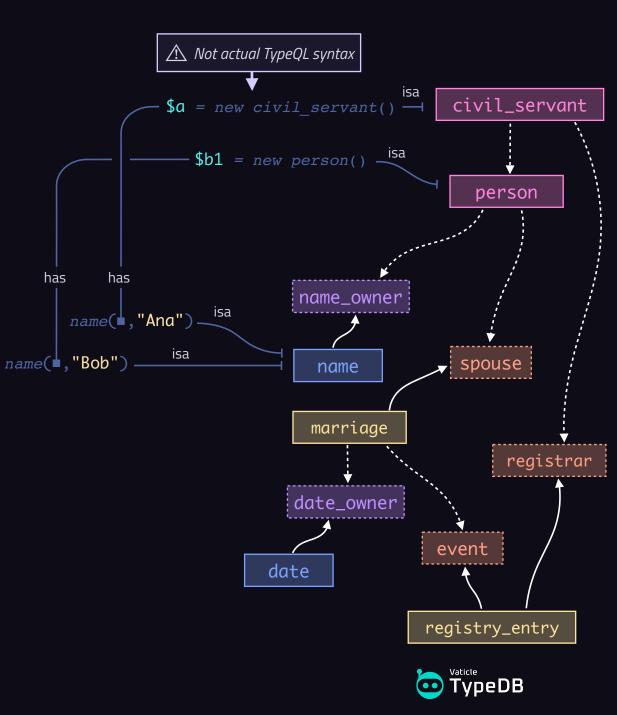
- For given type schema can
 insert data instances
- Must account for value types and dependencies



- For given type schema can
 insert data instances
- Must account for value types and dependencies



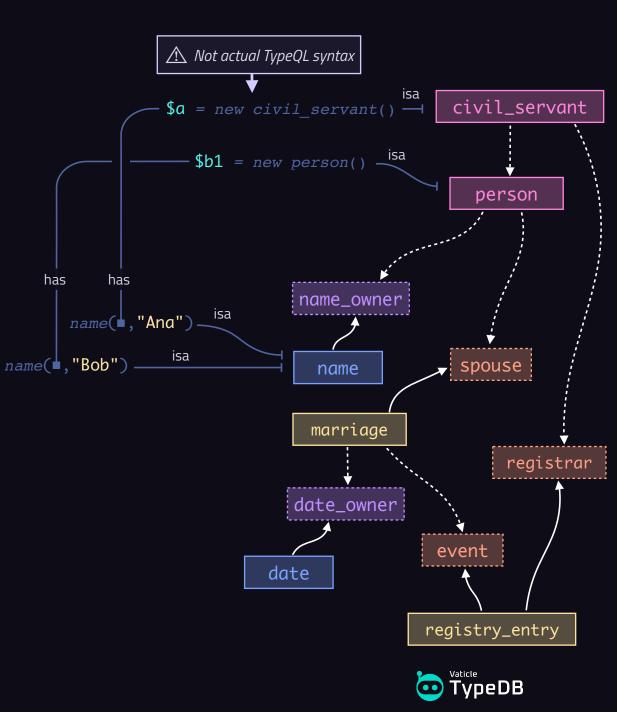
- For given type schema can insert data instances
- Must account for value types and dependencies



- For given type schema can insert data instances
- Must account for value types and dependencies

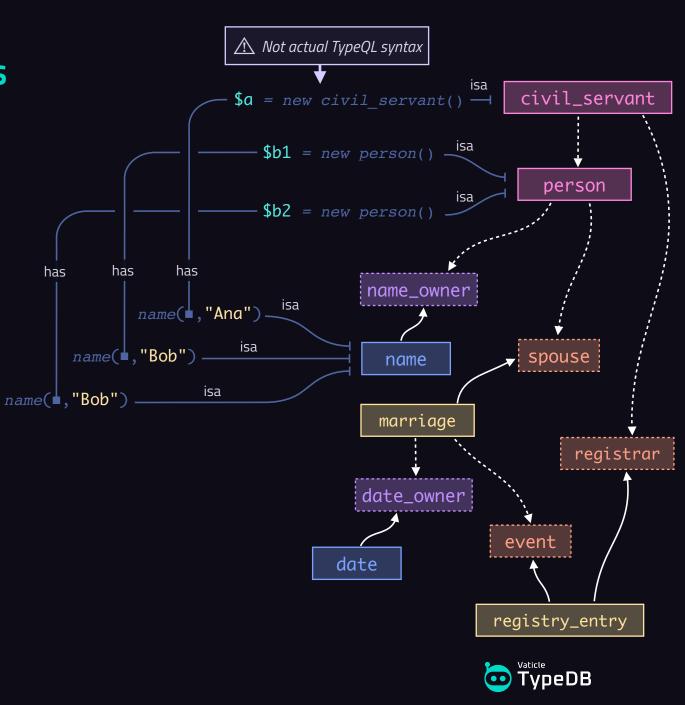
insert \$a isa civil_servant; \$a has name "Ana"; \$b1 isa person, has name "Bob"; \$b2 isa person, has name "Bob";

- \$m (spouse: \$b1, spouse: \$b2)
 isa marriage,
- nas date 17-05-2004; (event: \$m, registrar: \$a
 - isa registry_entry;



- For given type schema can insert data instances
- Must account for value types and dependencies

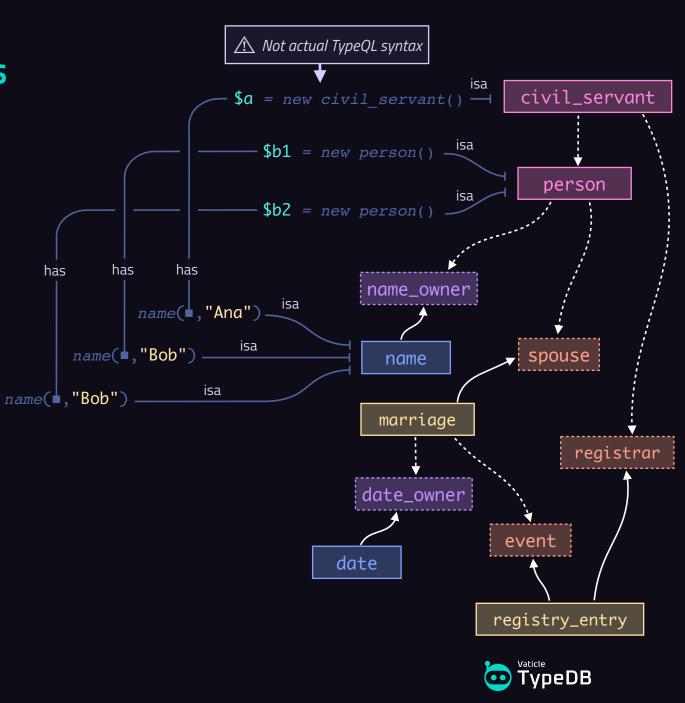
```
insert
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



TypeQL practice: data instances

- For given type schema can insert data instances
- Must account for value types and dependencies

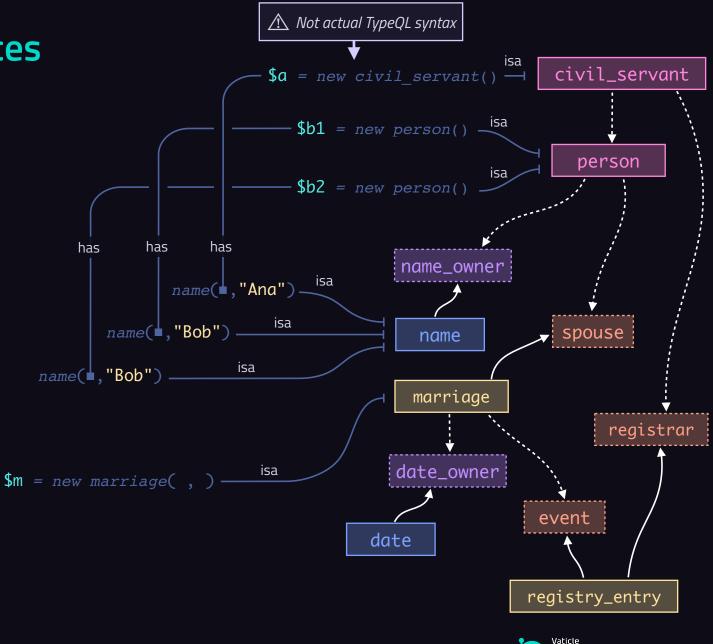
```
insert
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



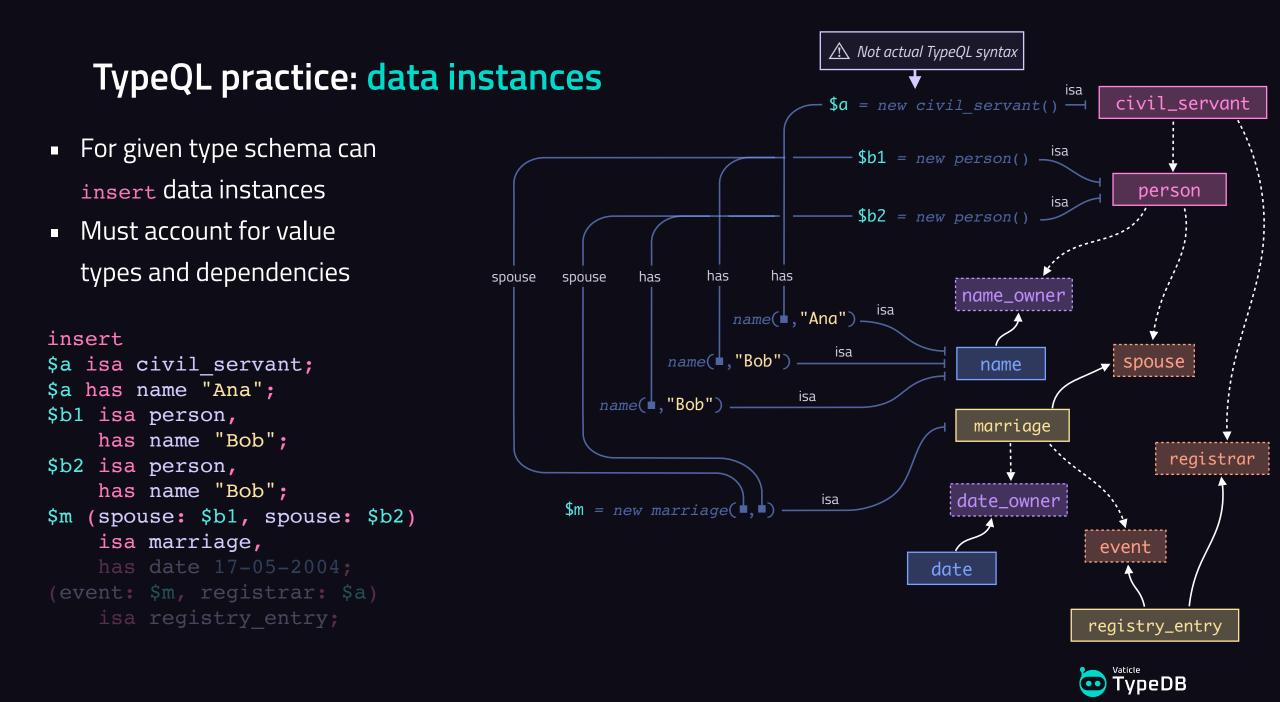
TypeQL practice: data instances

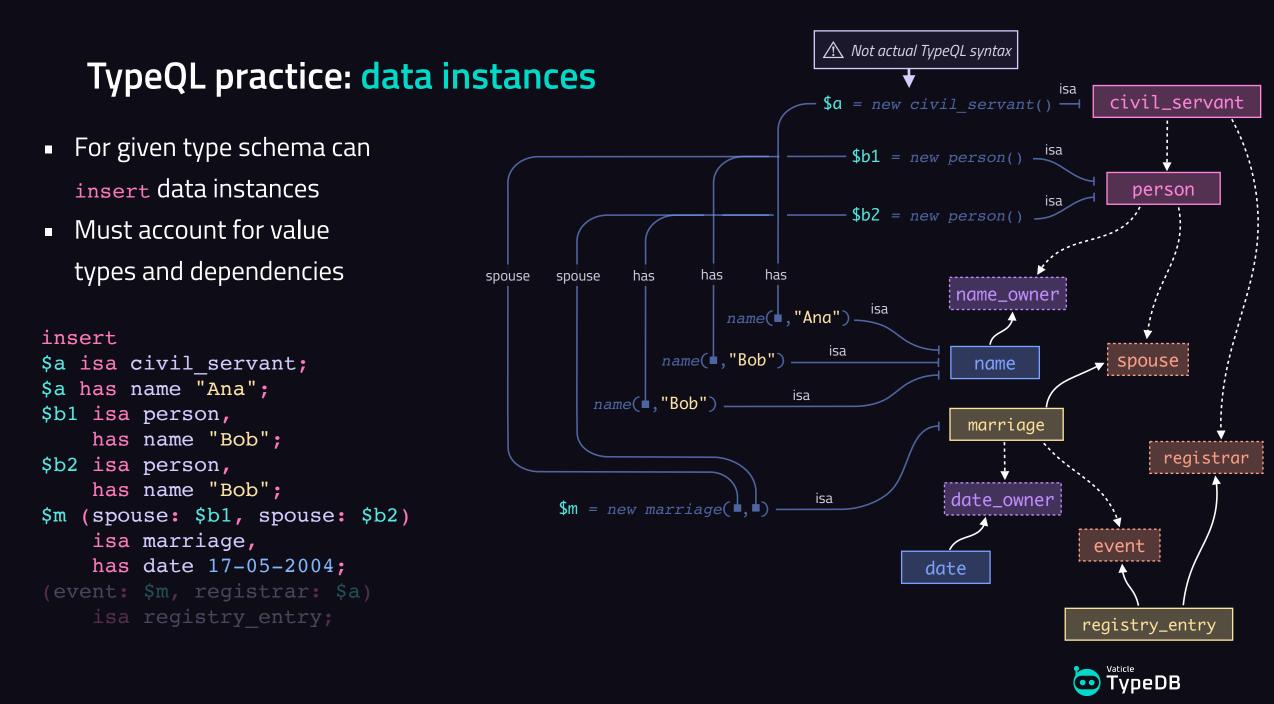
- For given type schema can insert data instances
- Must account for value types and dependencies

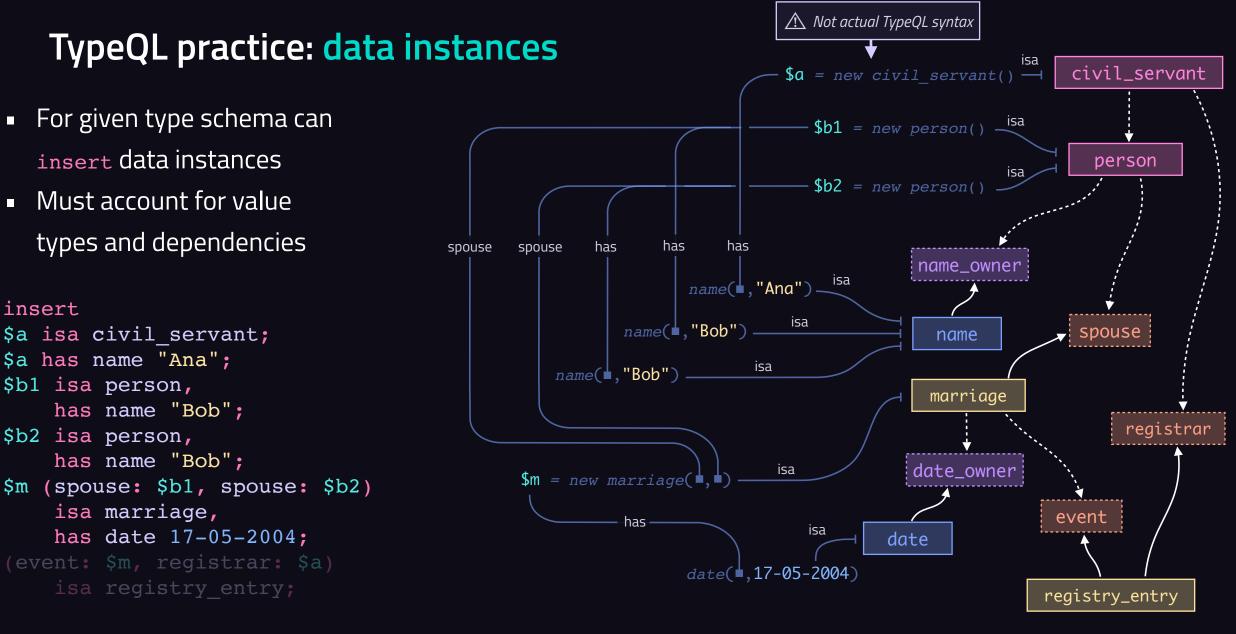
```
insert
$a isa civil_servant;
$a has name "Ana";
$b1 isa person,
    has name "Bob";
$b2 isa person,
    has name "Bob";
$m (spouse: $b1, spouse: $b2)
    isa marriage,
    has date 17-05-2004;
(event: $m, registrar: $a)
    isa registry_entry;
```



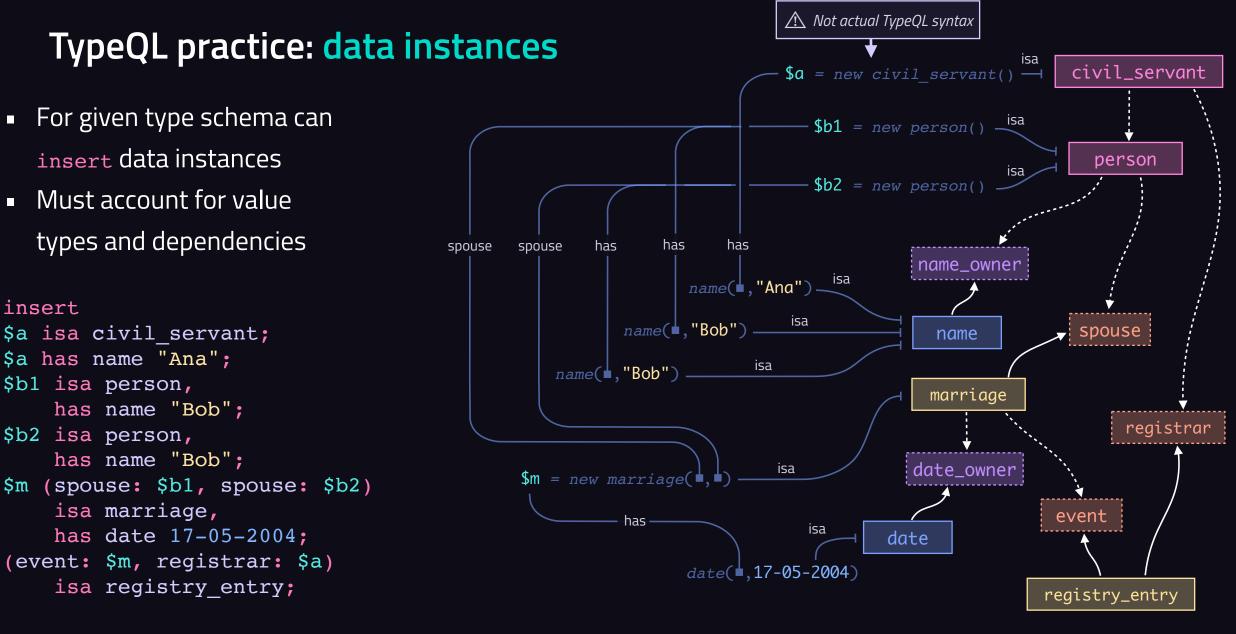
ΓνοεDΒ



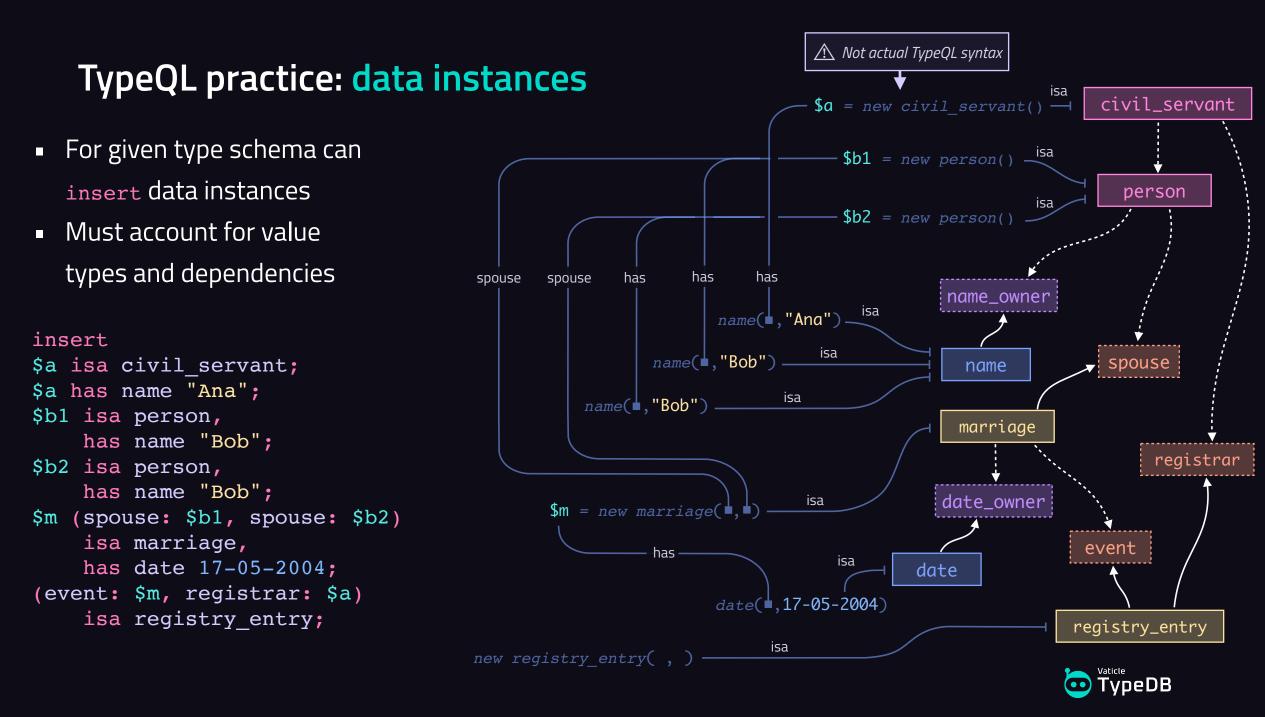


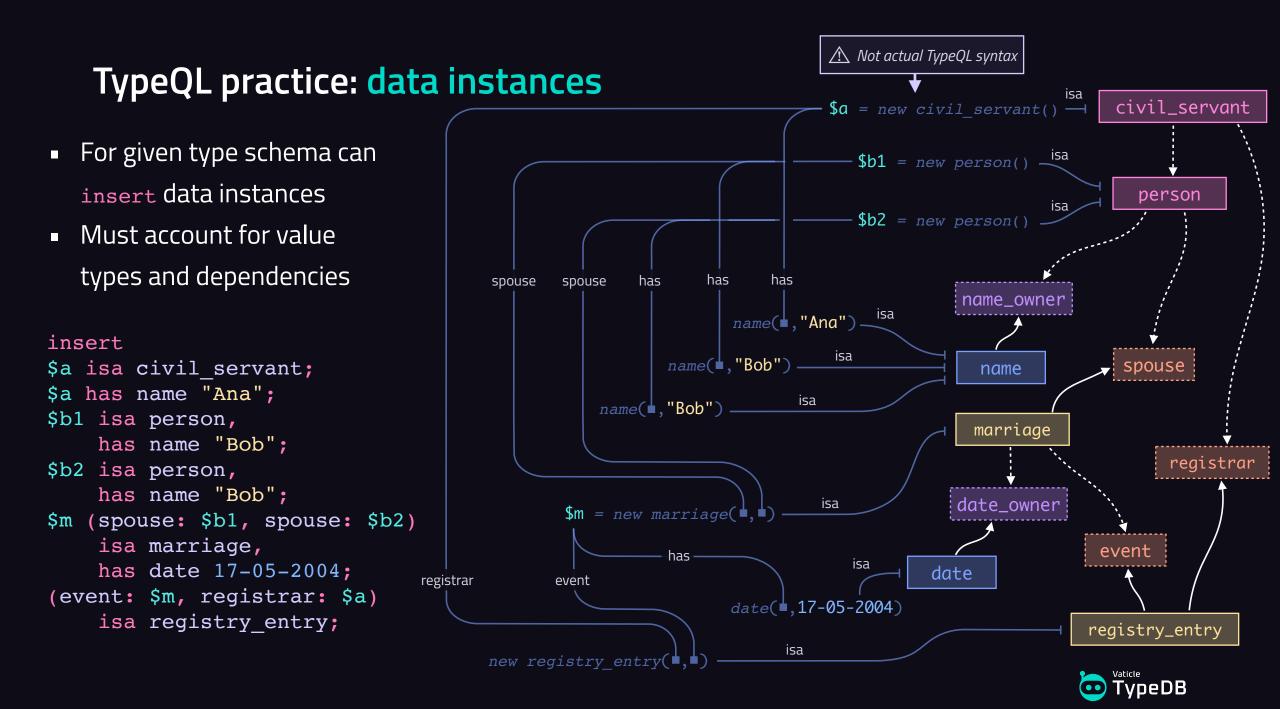












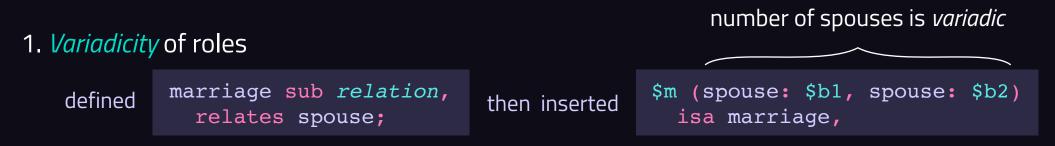
TypeQL practice: data instances—*the details*

1. *Variadicity* of roles

defined	<pre>marriage sub relation, relates spouse;</pre>	then inserted	<pre>\$m (spouse: \$b1, spouse: \$b2) isa marriage,</pre>
---------	---	---------------	---



TypeQL practice: data instances — *the details*







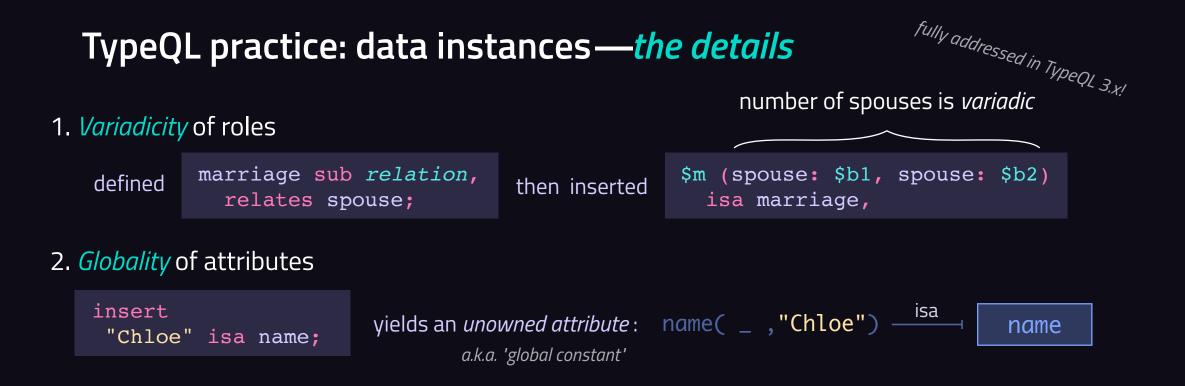




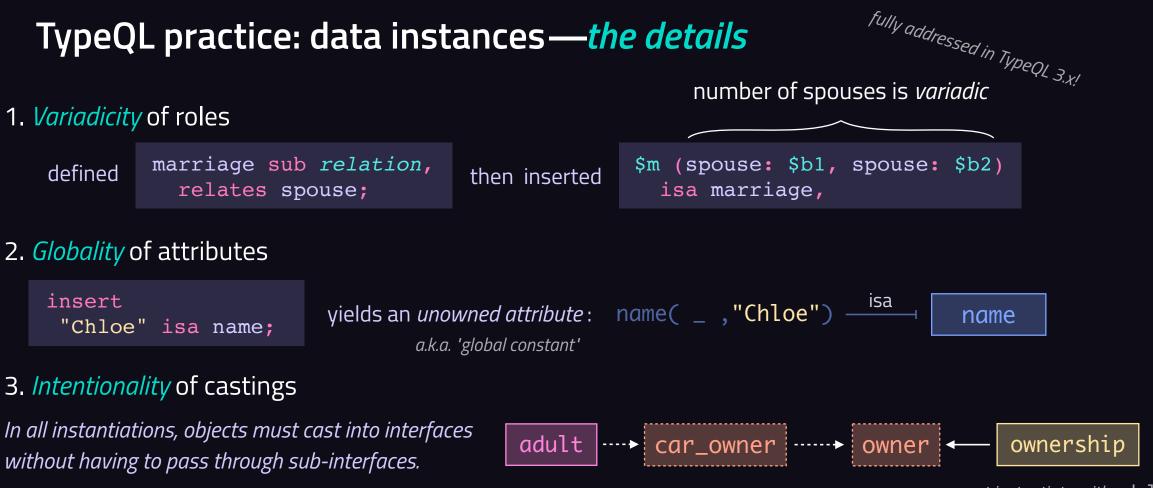
2. *Globality* of attributes

insert "Chloe" isa name;



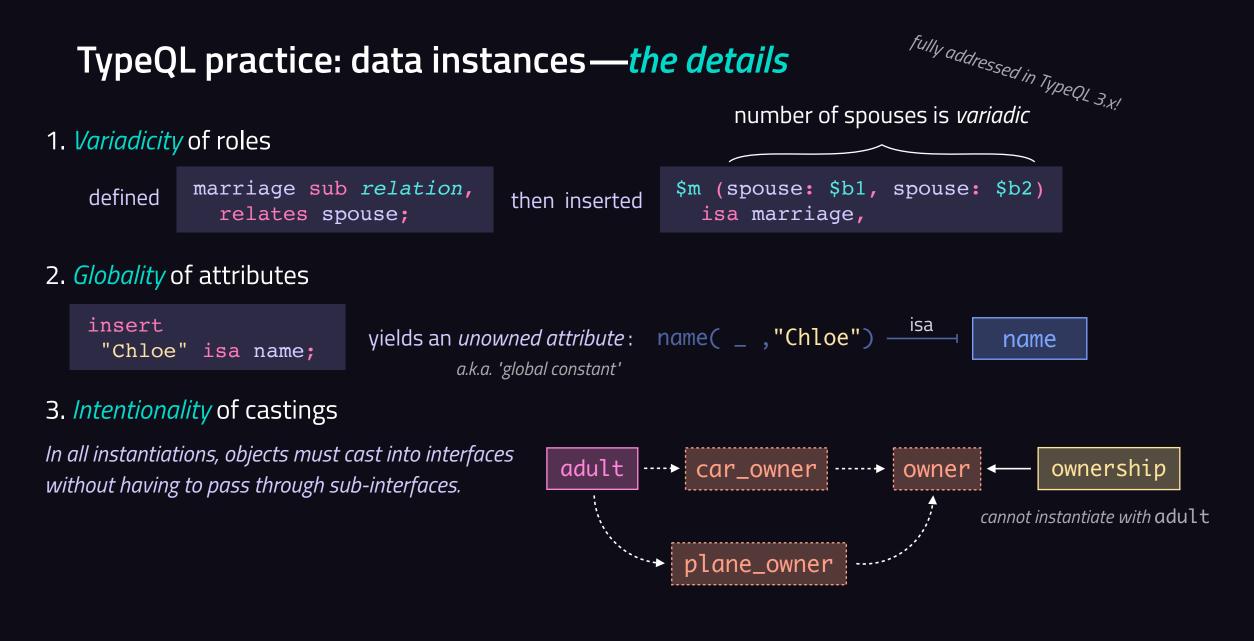






cannot instantiate with adult









• The PERA type system as *three* kinds of types:

	independent type	dependent type
object	optity types	rolation types
types	entity types	relation types
attribute	(global constants)	attributa tunas
types	(global constants)	attribute types



- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies

	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types

employee]▶	person
----------	----	--------



- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies
- All dependencies are abstracted by interface types

_	indep	endent t	ype	depende	ent type
object types	entity types		relation	n types	
attribute types	(global constants)		attribute types		
emplo	oyee	▶	р	erson	
		2 2			

name



- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies
- All dependencies are abstracted by interface types
- Object types can implement these interfaces

	independent type			depende	ent type
object	entity types		_	rolatio	
types			5	relatio	irtypes
attribute	(global constants		ntcl_	attribut	
types	lgiobi	u constai	11.57	attribute types	
employee ·····►		р	erson		
		1			
name_0				ame	

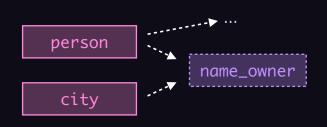




- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies
- All dependencies are abstracted by interface types
- Object types can implement these interfaces
- Single-inheritance but multi-capability via interfaces

	independent type		depende	ent type	
object	entity types (global constants)		relatior	n types	
types attribute types			attribute types		
emplo	oyee		р	erson	
		1			

name

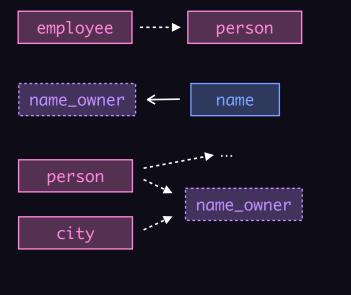


name owne



- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies
- All dependencies are abstracted by interface types
- Object types can implement these interfaces
- Single-inheritance but multi-capability via interfaces
- Objects in object types can be freely created

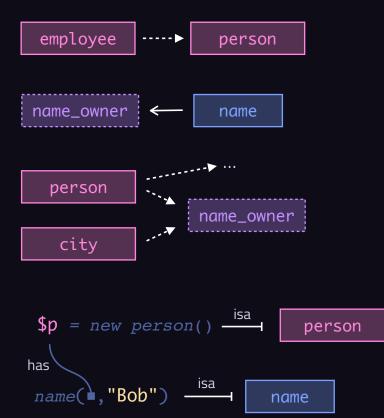
	independent type	dependent type	
object	optity types	rolation types	
types	entity types	relation types	
attribute	(global constants)	attribute types	
types	(giobai constants)	attribute types	





- The PERA type system as *three* kinds of types:
- Type kinds are organized by inheritance hierarchies
- All dependencies are abstracted by interface types
- Object types can implement these interfaces
- Single-inheritance but multi-capability via interfaces
- Objects in object types can be freely created
- Values can be (idempotently) added to attribute types

	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types





Part III: Comparison to other data models

...and how PERA brings order to modeling



The bottomline



The bottomline

The PERA model is a *simple and principled* model, built on basic and fundamental ideas found across *all* data models. From the PERA perspective, capturing other data models is *easy*.





Instances:

employee		
name	member_of	
"Ana"	1	
"Bob"	1	
"Chloe"	Ŷ	

team			
id	team_name		
1	"Engineering"		
2	"Marketing"		
3	"Research"		

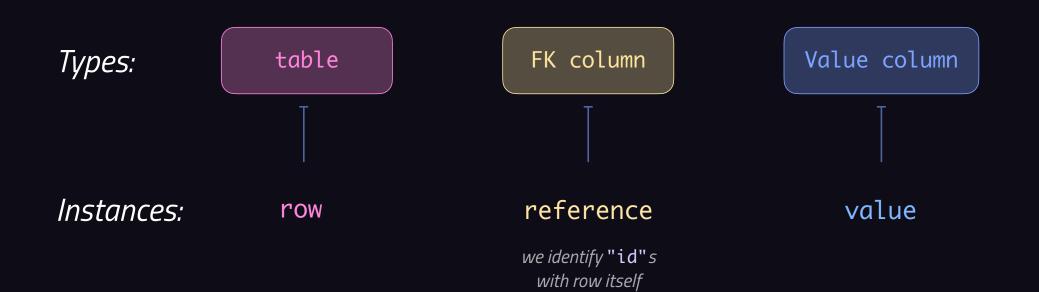




employee		
name	member_of	
"Ana"	1	
"Bob"	1	
"Chloe"	Z	

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"

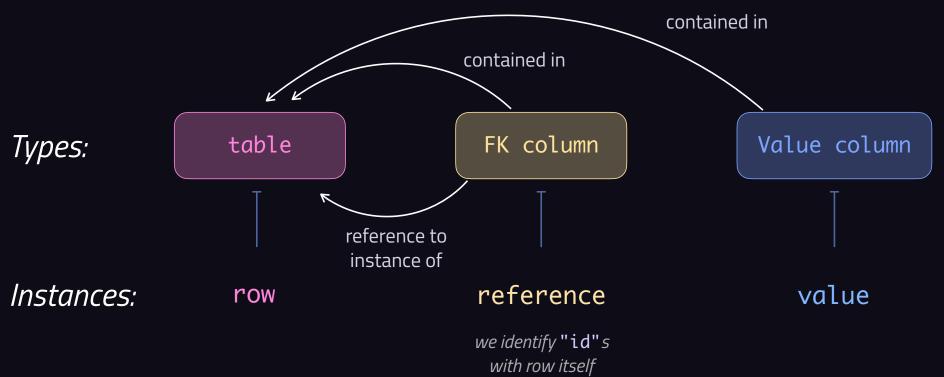




employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	3

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"

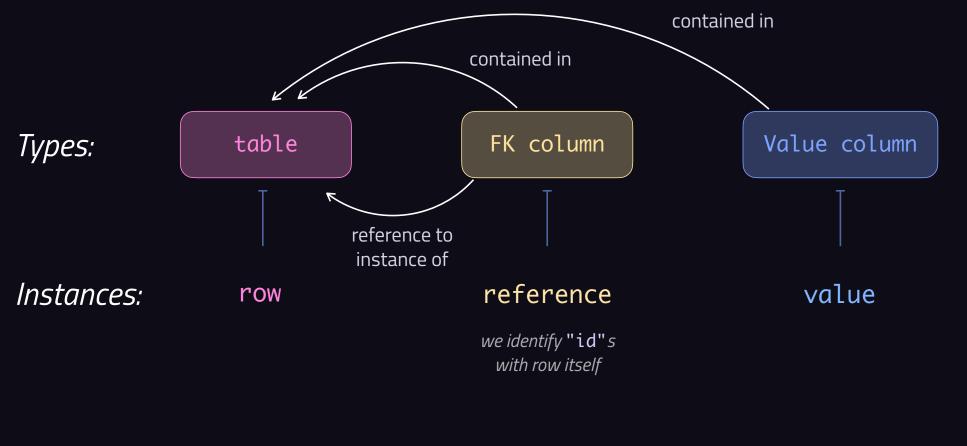




employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	2

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"



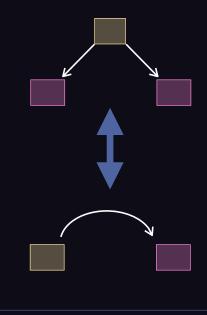


employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloo"	3

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"

Remark. Constraints can modify dependencies!

e.g. NOT NULL FK:





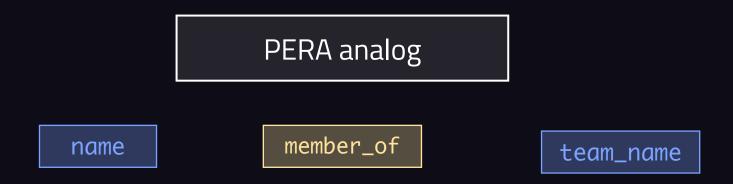
employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	3
•••	•••

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"
• • •	

PERA analog



employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	3
• • •	• • •



team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"
• • •	•••

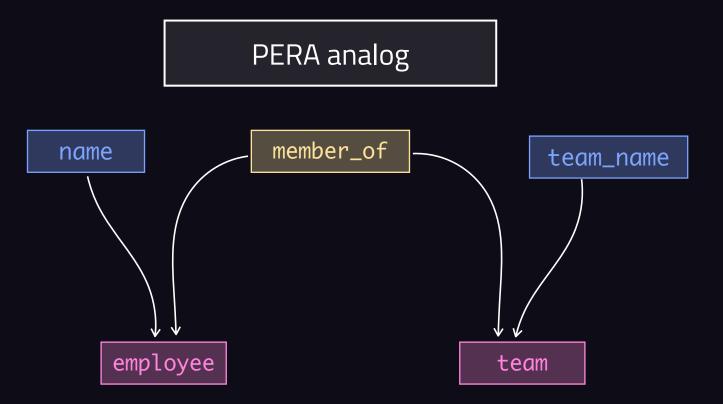






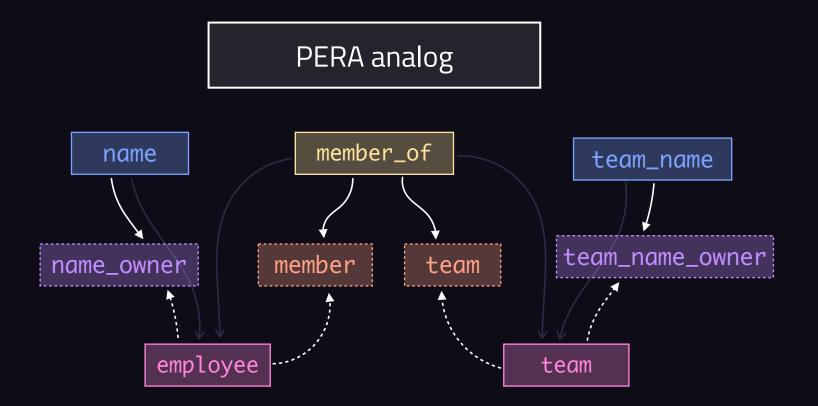
employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	3
• • •	• • •

team		
id	team_name	
1	"Engineering"	
2	"Marketing"	
3	"Research"	
• • •	• • •	





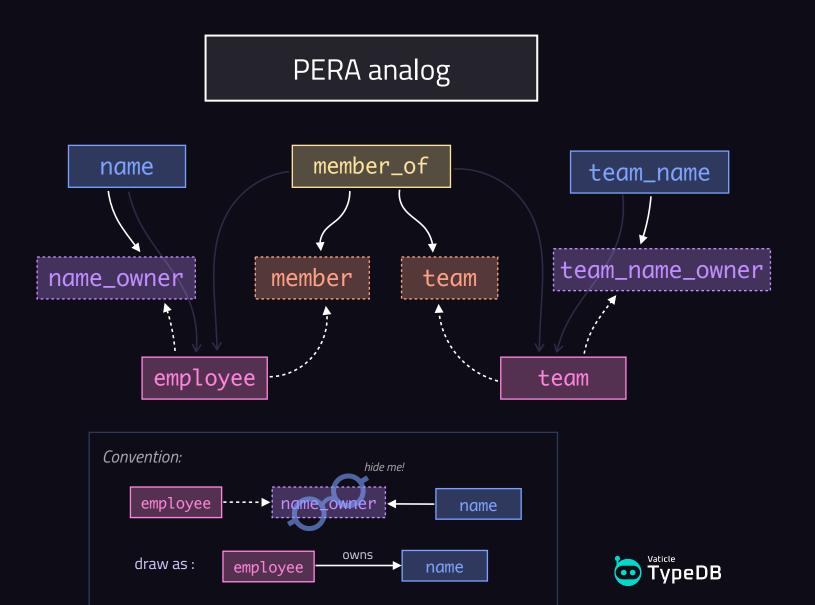
employee		
name	member_of	
"Ana"	1	
"Bob"	1	
"Chloe"	3	
• • •	• • •	



team		
id	team_name	
1	"Engineering"	
2	"Marketing"	
3	"Research"	
• • •	• • •	



employee		
name	member_of	
"Ana"	1	
"Bob"	1	
"Chloe"	3	
• • •	• • •	

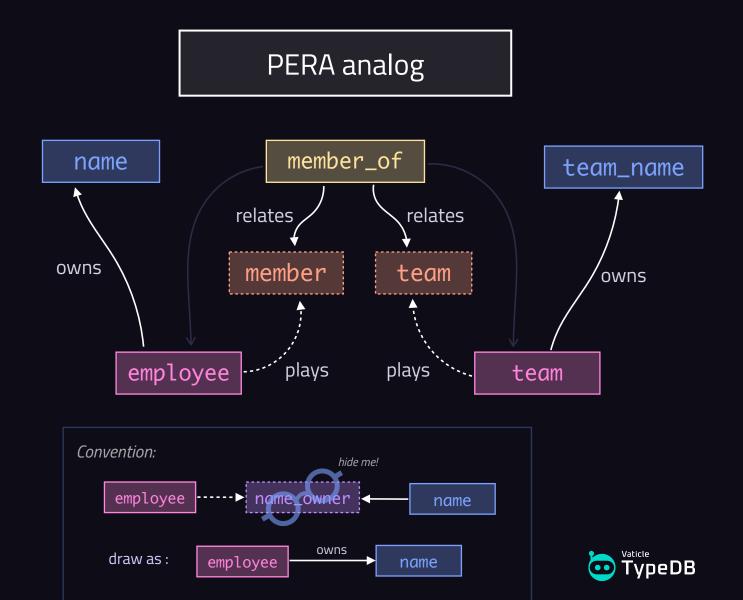


team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"
• • •	• • •

The relational model: a simple example

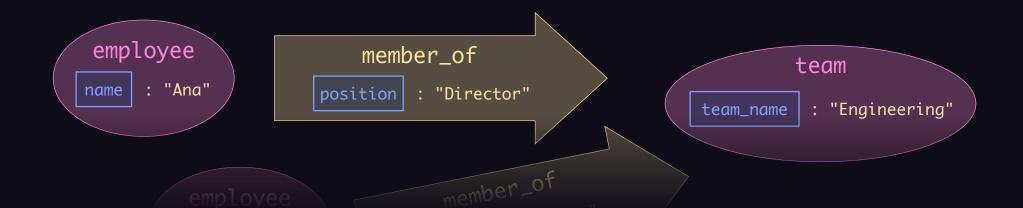
employee	
name	member_of
"Ana"	1
"Bob"	1
"Chloe"	3
• • •	• • •

team	
id	team_name
1	"Engineering"
2	"Marketing"
3	"Research"
• • •	

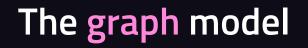


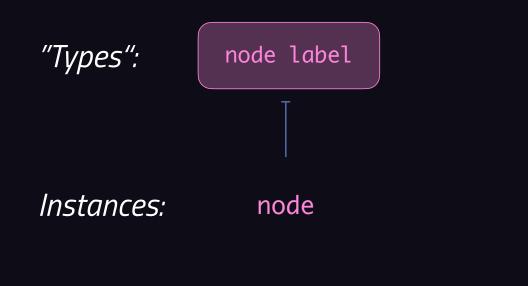
"Types":

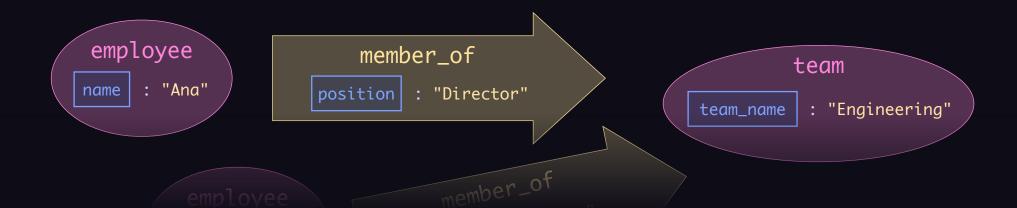
Instances:



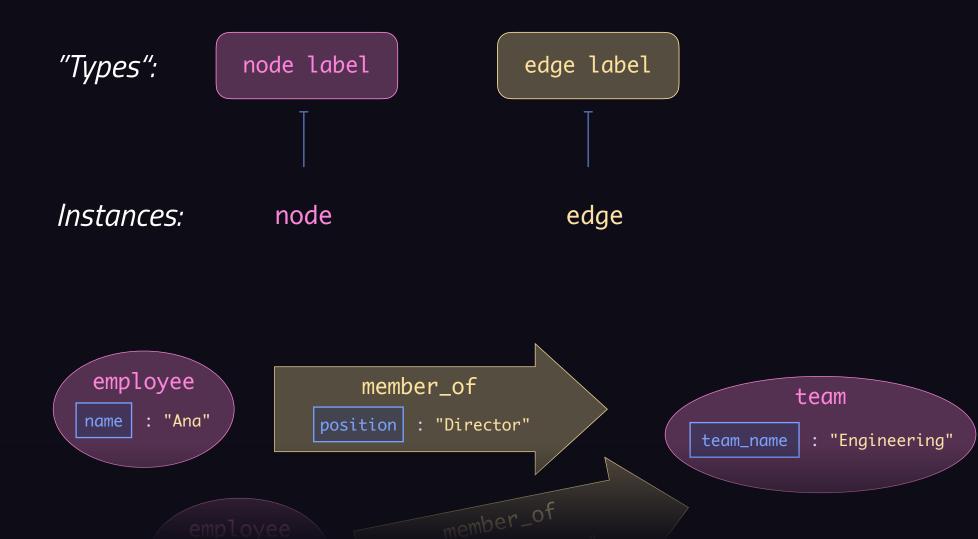






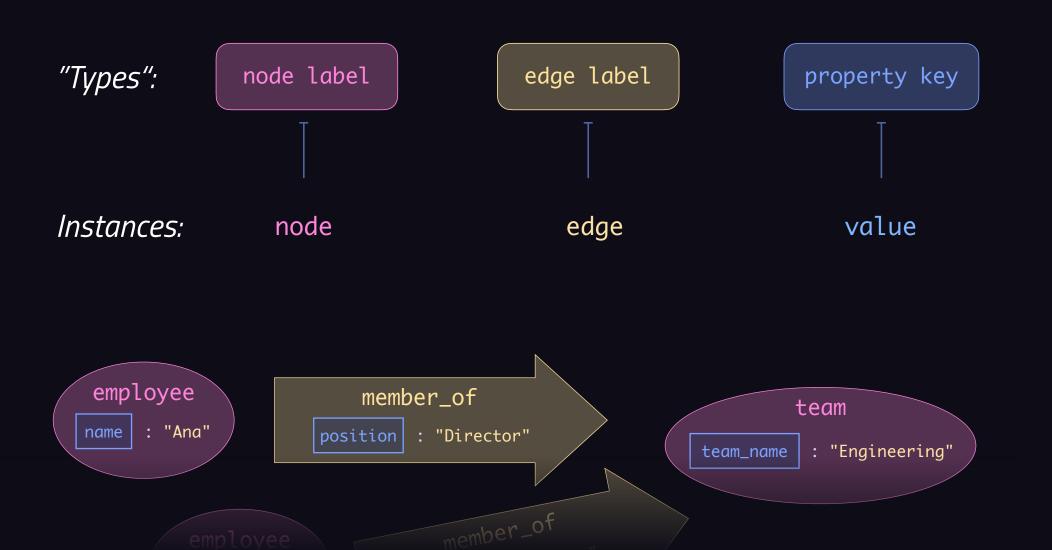






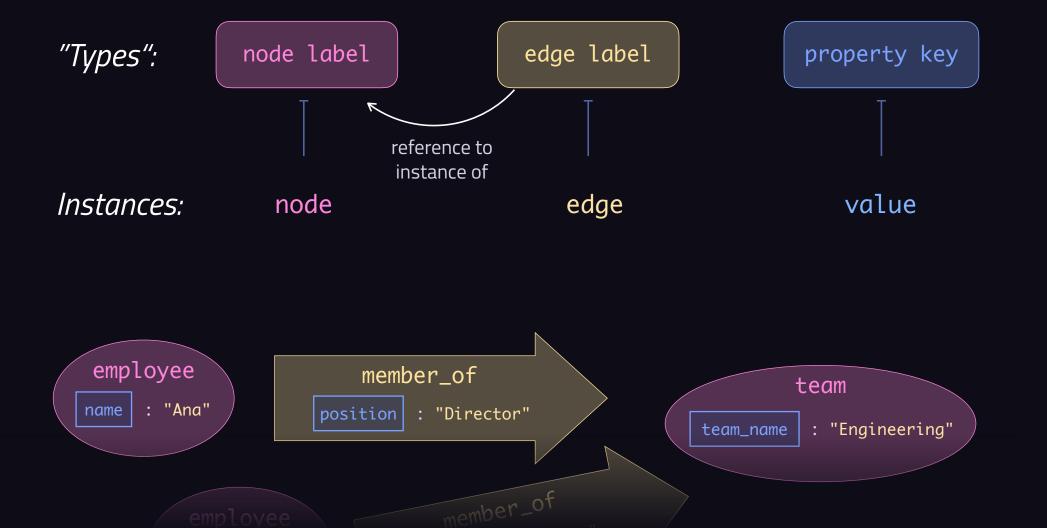
TypeDB

 $\textcircled{}$



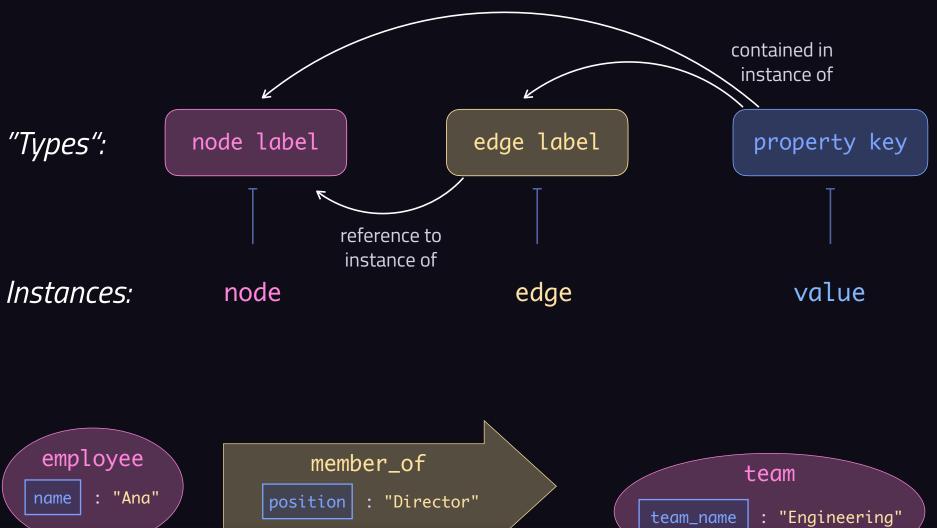
TypeDB

 \bigcirc

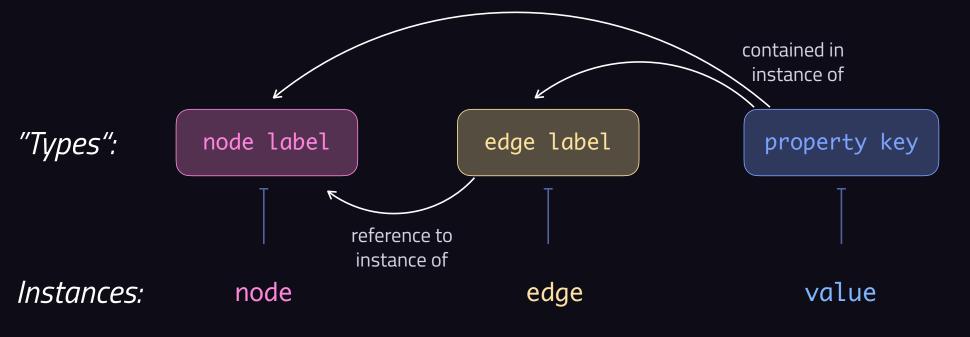


TypeDB

 \bigcirc



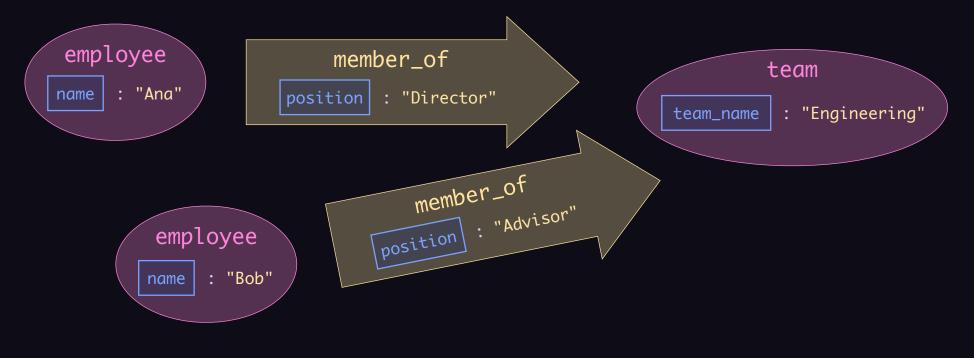




Remark. In the LPG, nodes and edges can be assigned multiple labels, which emulates "subtype hierarchies". However, this provides no meaningful way to model inheritance of type behaviors.

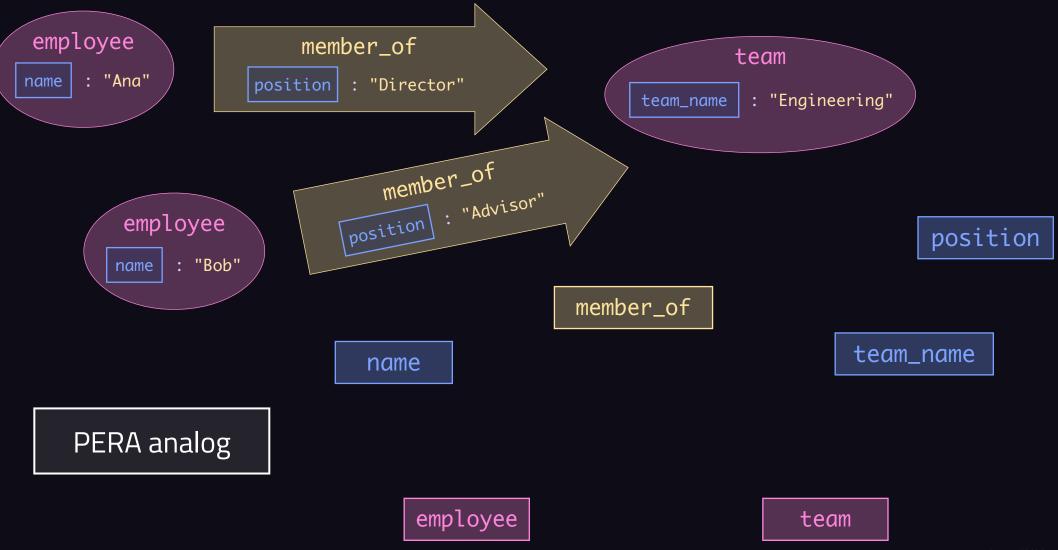




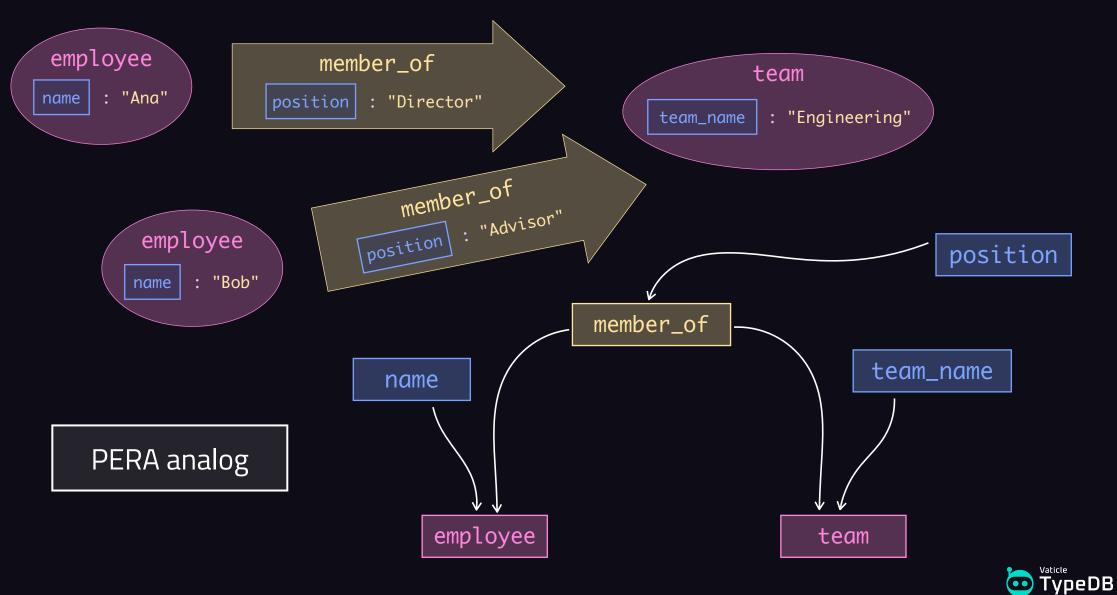


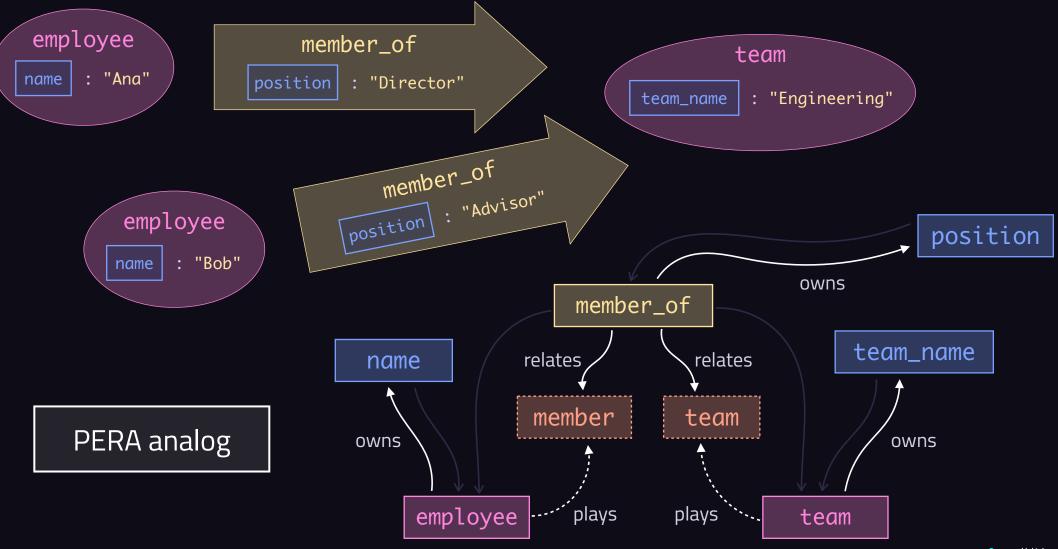
PERA analog







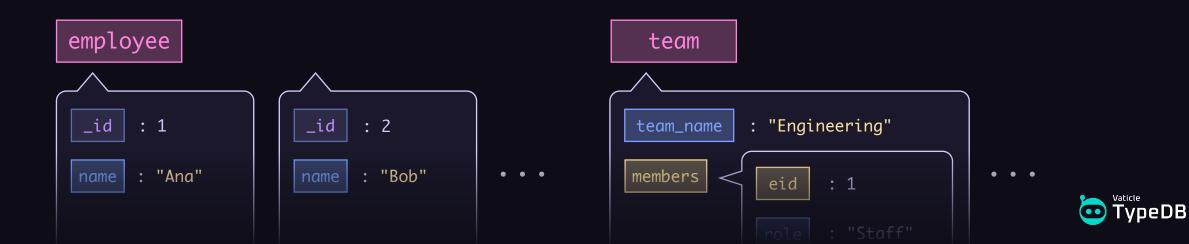


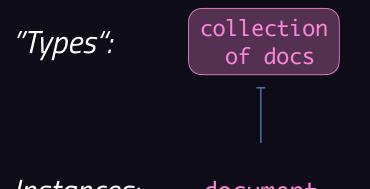




"Types":

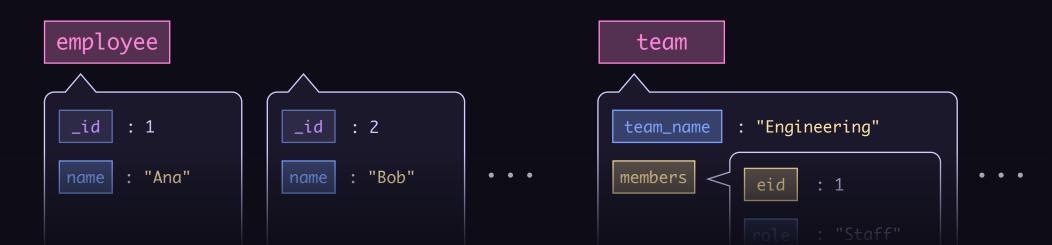
Instances:



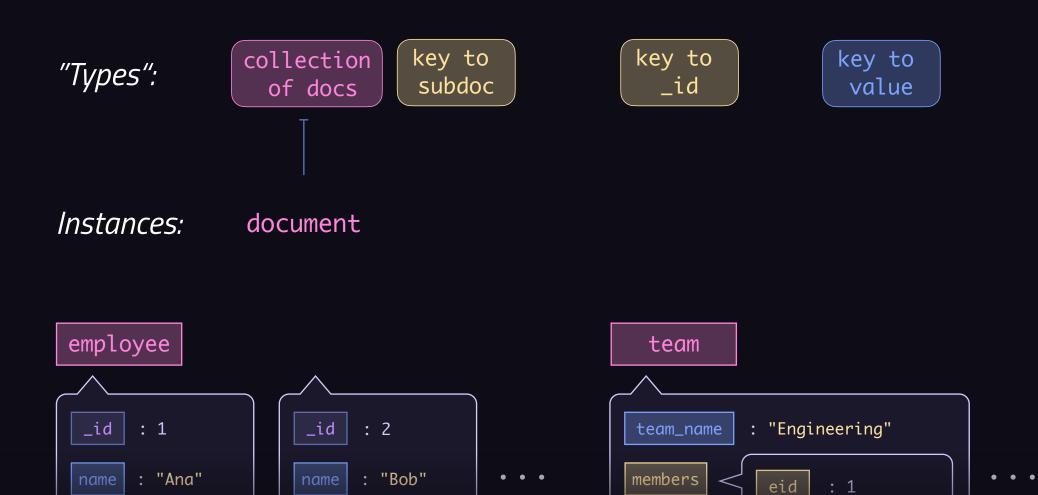


Instances:

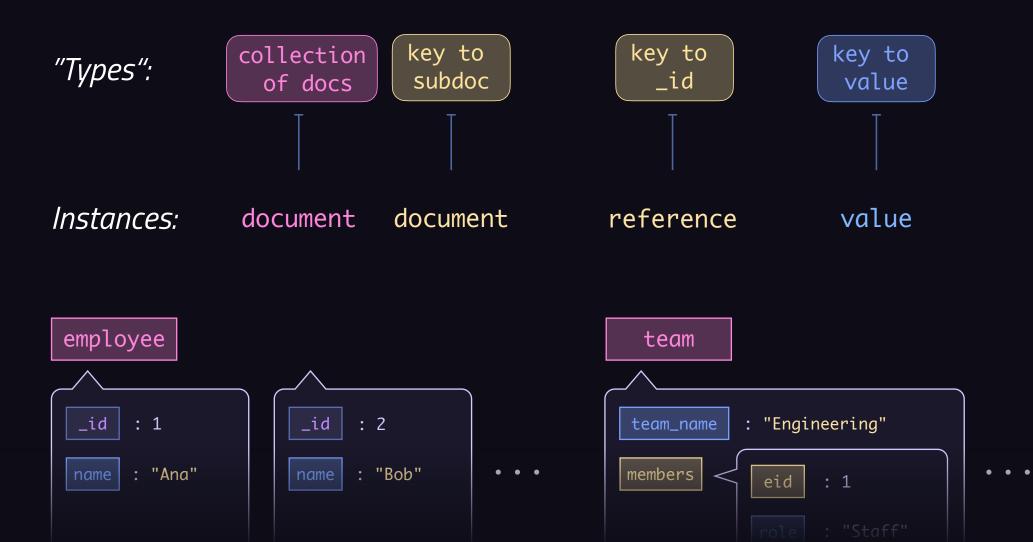
document





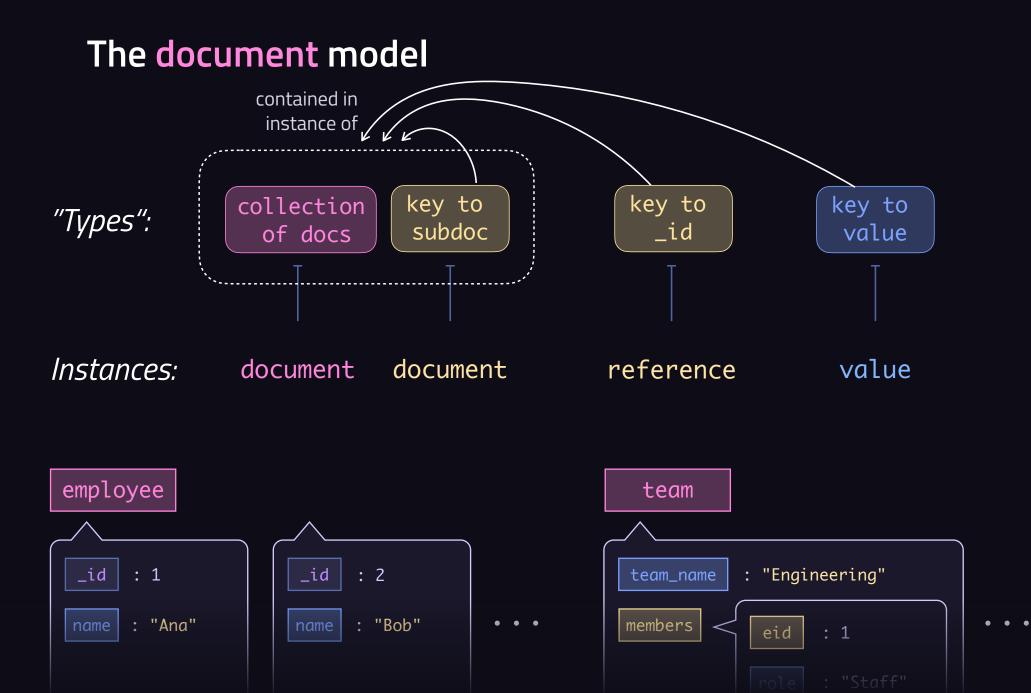




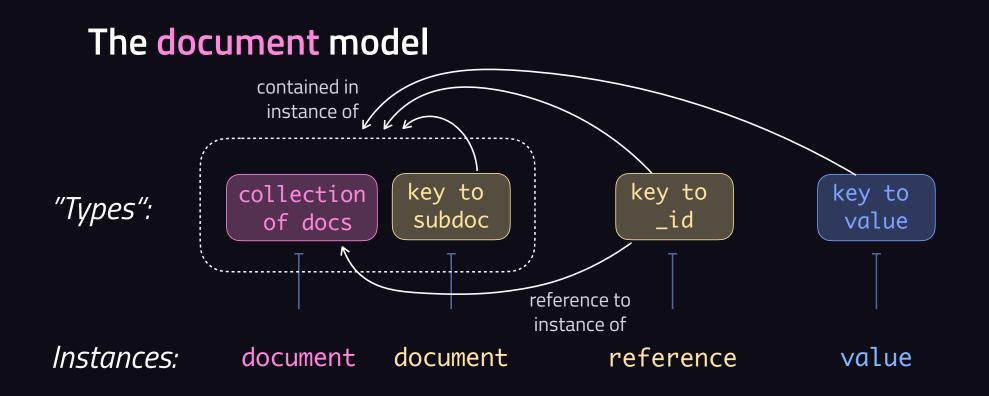


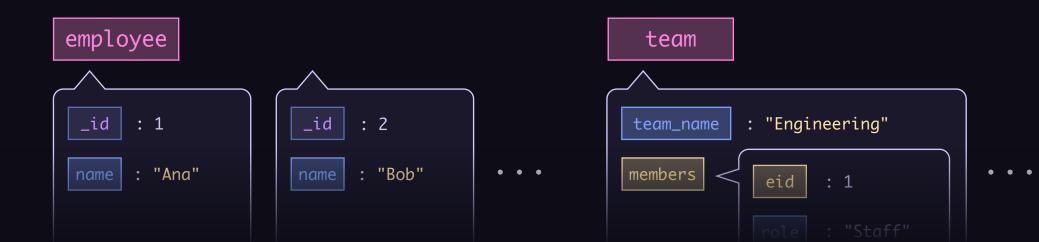
TypeDB

 \bigcirc

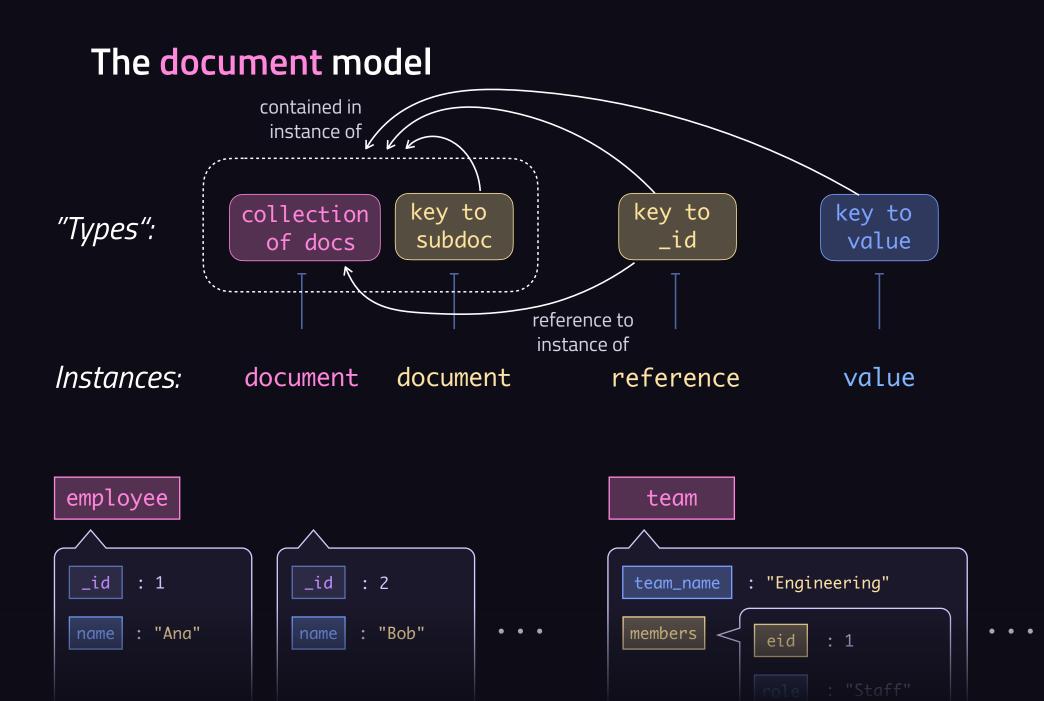






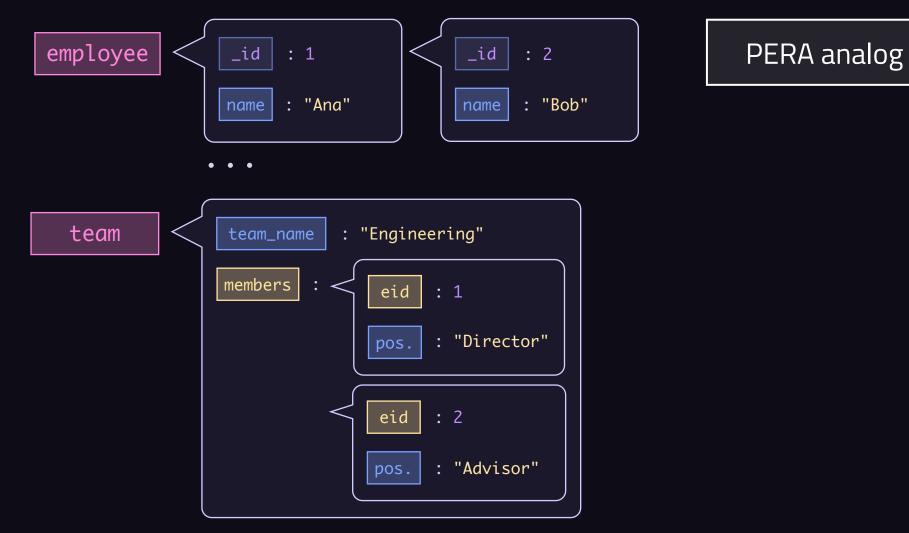




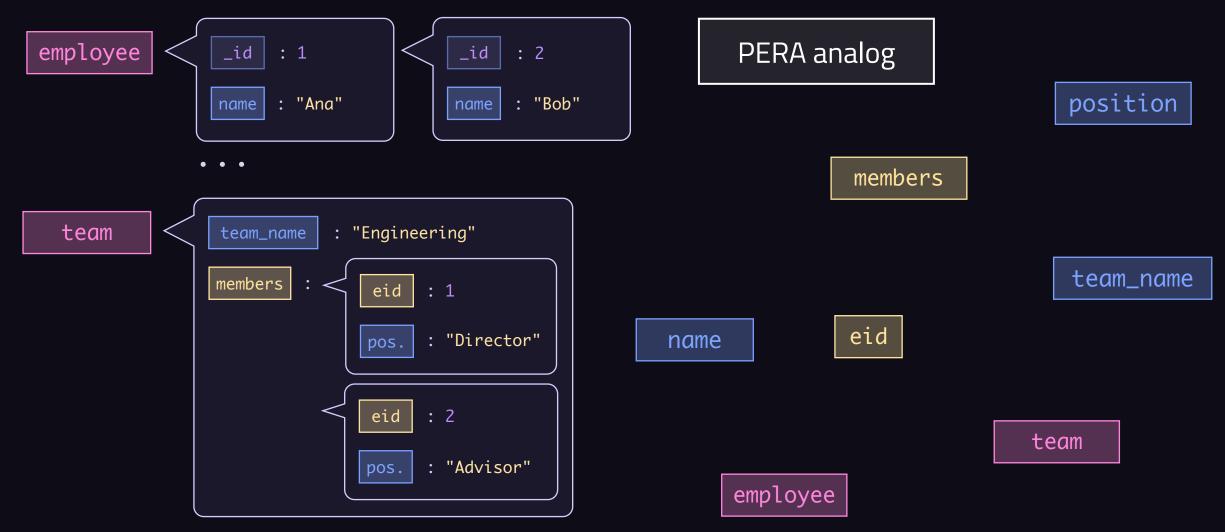


Remark. Semantically, some embedded subdocuments represent *duplicates* of other documents, but the document model does not relate these logically independent data instances.

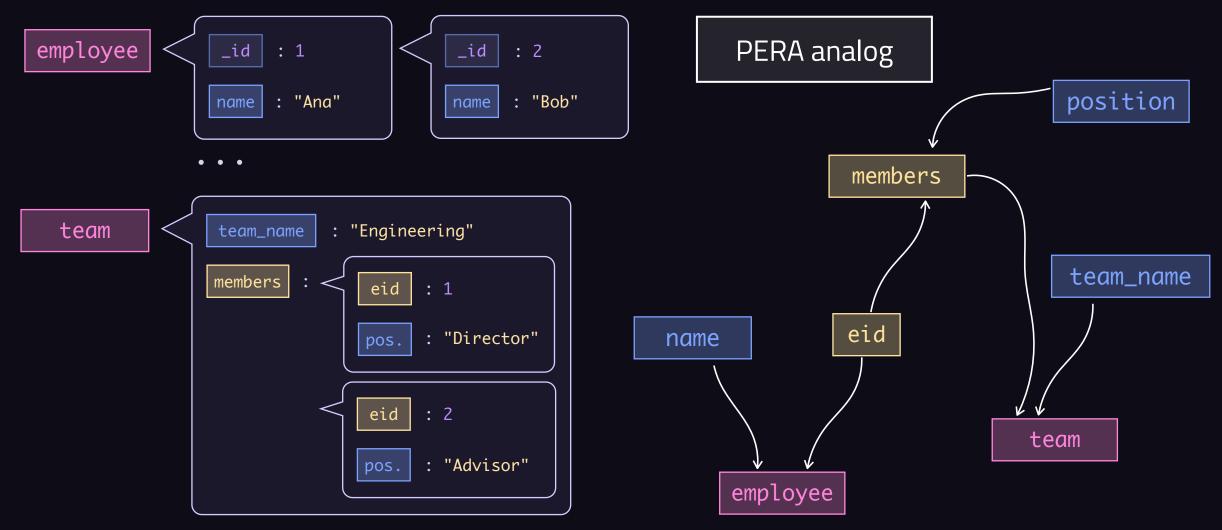




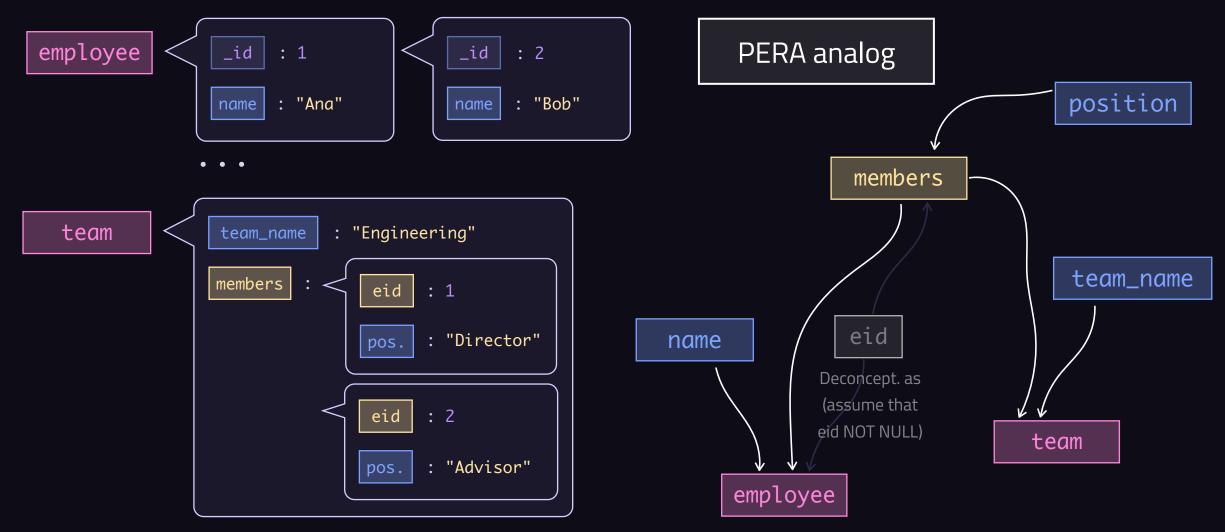




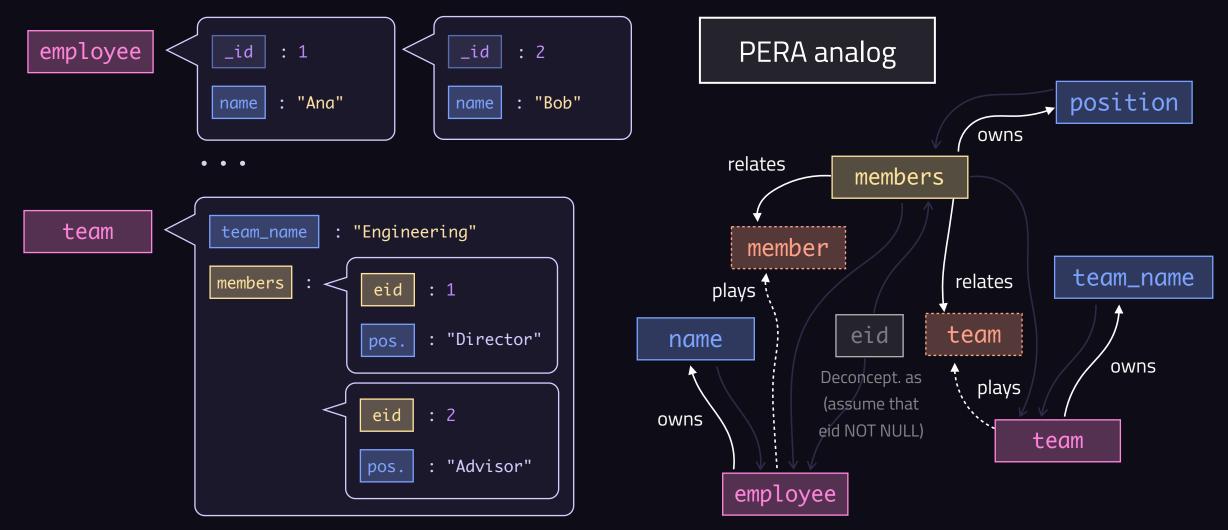




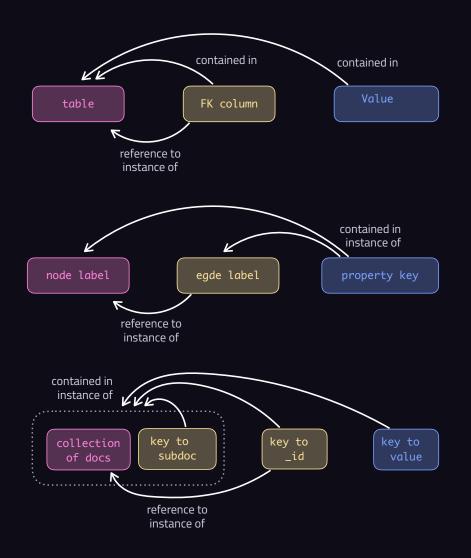




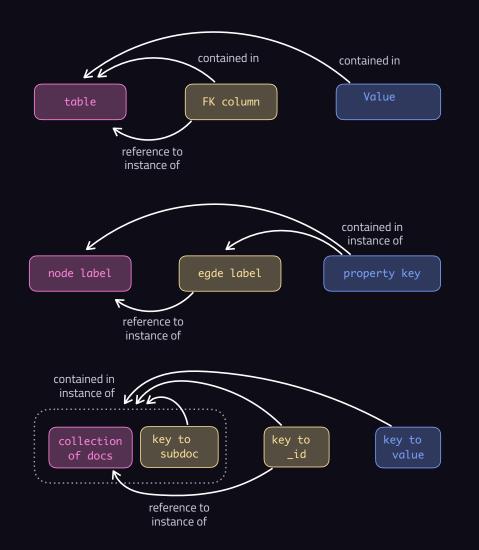
TypeDB





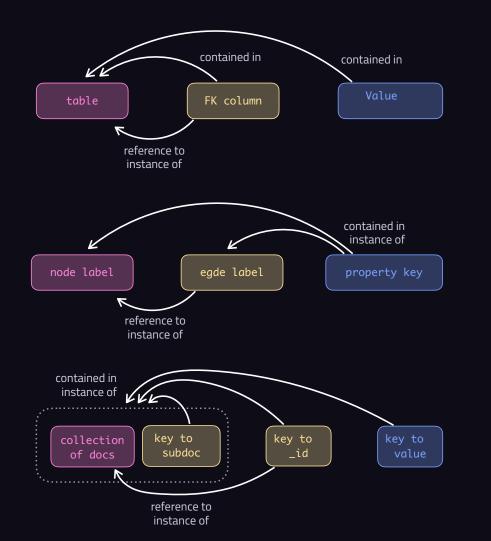


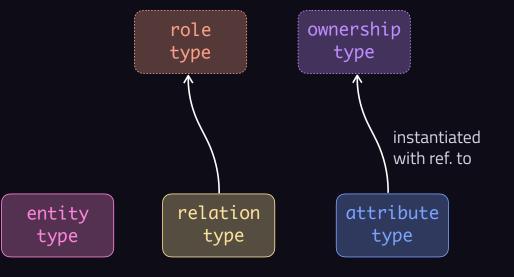




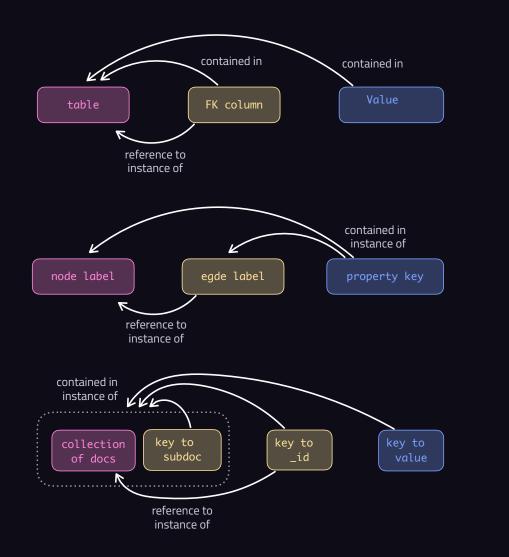


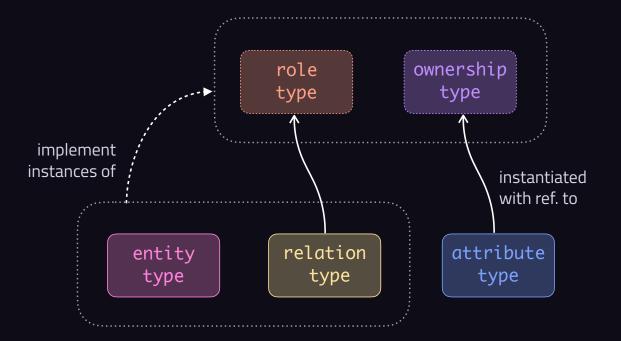




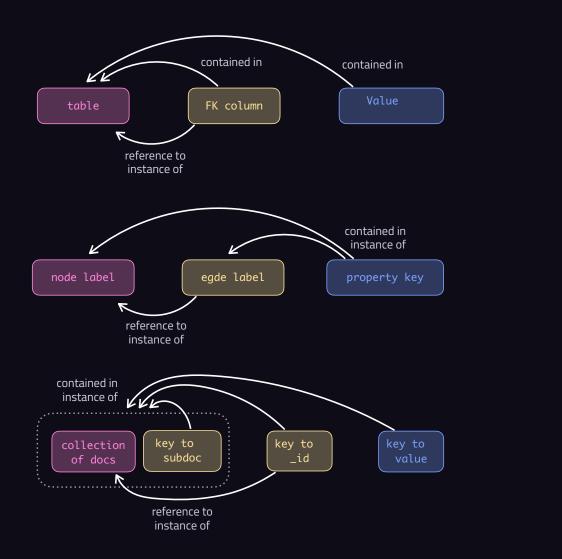


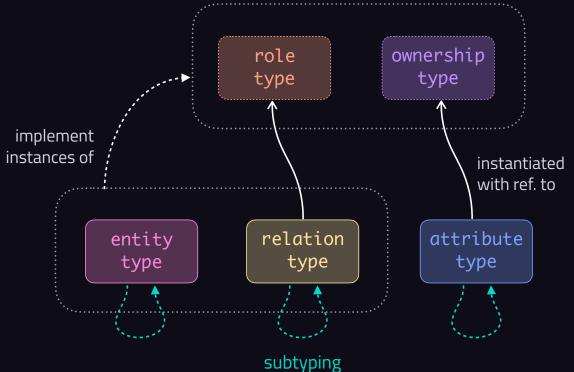




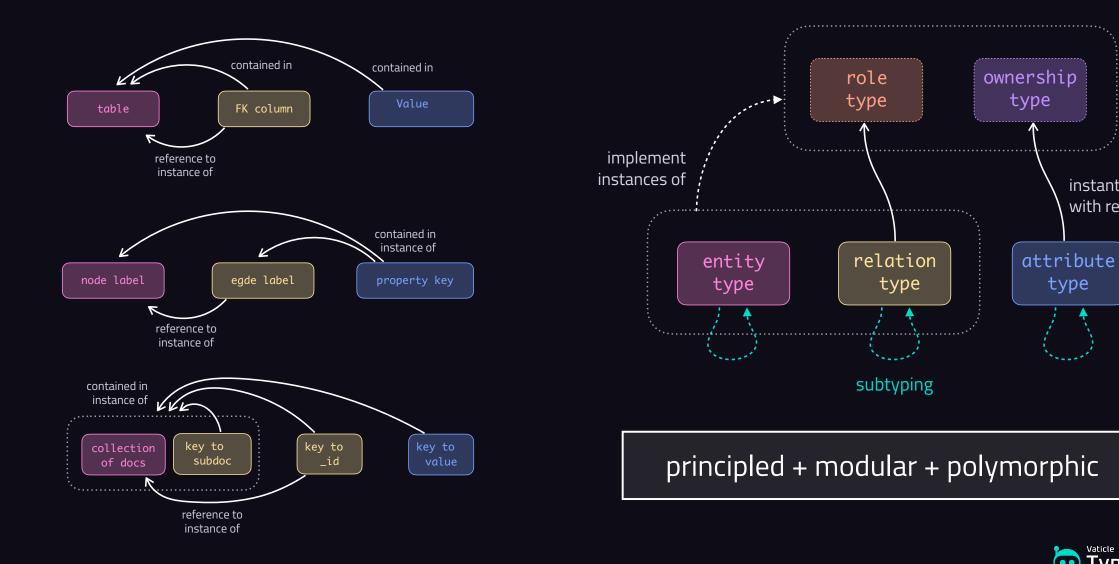














instantiated with ref. to



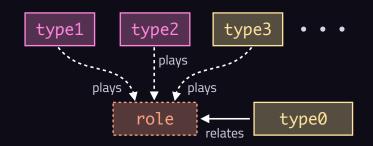
In comparison to other data models, the PERA model is



- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function

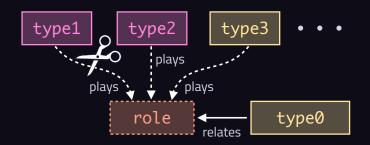


- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function
 - Modular: safely modify implementations of dependencies



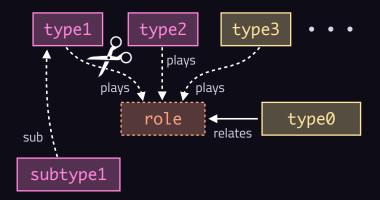


- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function
 - Modular: safely modify implementations of dependencies





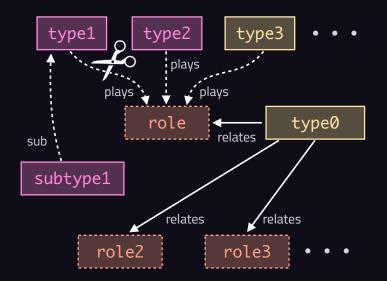
- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function
 - Modular: safely modify implementations of dependencies
 - *Polymorphic*: directly express type capabilities and type inheritance





Summary and further remarks

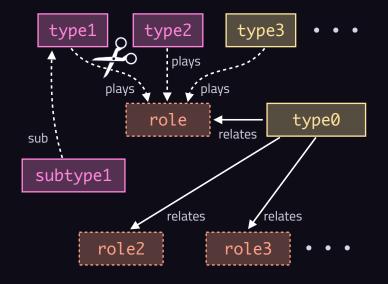
- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function
 - Modular: safely modify implementations of dependencies
 - *Polymorphic*: directly express type capabilities and type inheritance
 - ... and more: variadicity, globality, ...

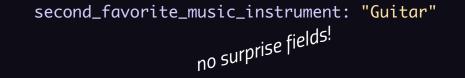




Summary and further remarks

- In comparison to other data models, the PERA model is
 - *Principled*: types have explicit and unambiguous function
 - Modular: safely modify implementations of dependencies
 - *Polymorphic*: directly express type capabilities and type inheritance
 - ... and more: variadicity, globality, ...
- The PERA model follows a *type-first approach*
 - In schema-less approaches types are an *after-thought*
 - Requires us to think about types *ahead of time*, but modularity makes *continuous development* painless







Epilogue: Beyond the basics

Polymorphic *pattern-based* querying and reasoning





- *Type-theoretic querying*
 - Queries via patterns ... patterns via types
 - Elegant and intuitive querying paradigm



- Type-theoretic querying
 - Queries via patterns ... patterns via types
 - Elegant and intuitive querying paradigm

"data type of solutions"

→ fully declarative QL



- Type-theoretic querying
 - Queries via patterns ... patterns via types
 - Elegant and intuitive querying paradigm
- Type-theoretic reasoning
 - Type system is a collection of rules (e.g.: subtyping)
 - User-defined rules can extend this to derive new data

"data type of solutions"

→ fully declarative QL



- Type-theoretic querying
 - Queries via patterns ... patterns via types
 - Elegant and intuitive querying paradigm
- *Type-theoretic reasoning*
 - Type system is a collection of rules (e.g.: subtyping)
 - User-defined rules can extend this to derive new data

Both are key functions of the PERA model ...let's give a brief preview!

"data type of solutions"

→ fully declarative QL



match

\$eng_team isa team, has team_name "Engineering";
 (team: \$eng_team, member: \$m) isa team_membership;
fetch

\$m as engineer: name;



match

\$eng_team isa team, has team_name "Engineering";
 (team: \$eng_team, member: \$m) isa team_membership;
fetch

\$m as engineer: name;

Pattern

statements with variables that can be "solved for" by substituting objects and attributes for variables



```
match
    $eng_team isa team, has team_name "Engineering";
    (team: $eng_team, member: $m) isa team_membership;
fetch
    $m as engineer: name;
```

- match clause, line 1
 - Seng_team is some existing team object
 - that object must be the owner of the team_name "Engineering"

Pattern

statements with variables that can be "solved for" by substituting objects and attributes for variables



match \$eng_team isa team, has team_name "Engineering"; (team: \$eng_team, member: \$m) isa team_membership; fetch \$m as engineer: name;

- match clause, line 1
 - \$eng_team is some existing team object
 - that object must be the owner of the team_name "Engineering"
- match clause, line 2
 - there exists a team_membership object, left unassigned, but required to have a team roleplayer \$eng_team and a member roleplayer \$m

Pattern

statements with variables that can be "solved for" by substituting objects and attributes for variables



match \$ena te

\$eng_team isa team, has team_name "Engineering";
 (team: \$eng_team, member: \$m) isa team_membership;
fetch

\$m as engineer: name;

- match clause, line 1
 - **\$eng_team** is some existing team object
 - that object must be the owner of the team_name "Engineering"
- match clause, line 2
 - there exists a team_membership object, left unassigned, but required to have a team roleplayer \$eng_team and a member roleplayer \$m

Pattern

statements with variables that can be "solved for" by substituting objects and attributes for variables

What concept (i.e. type)
 does \$m belong to?

The answer is "polymorphic": \$m can belong to any type that implements the member role.



match

\$eng_team isa team, has team_name "Engineering";
 (team: \$eng_team, member: \$m) isa team_membership;
fetch

\$m as engineer: name;

- match clause, line 1
 - Seng_team is some existing team object
 - that object must be the owner of the team_name "Engineering"
- match clause, line 2
 - there exists a team_membership object, left unassigned, but required to have a team roleplayer \$eng_team and a member roleplayer \$m
- fetch clause, line 1
 - for each "engineer" object \$m return the name attribute(s) of \$m

Pattern

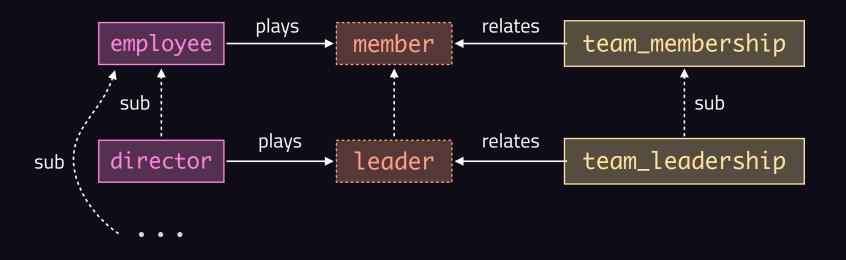
statements with variables that can be "solved for" by substituting objects and attributes for variables

What concept (i.e. type)
 does \$m belong to?

The answer is "polymorphic": \$m can belong to any type that implements the member role.



```
match
    $e isa employee;
    (team: $t, leader: $e) isa team_leadership;
fetch
    $e as leader: name;
    $t as team: team_name;
```

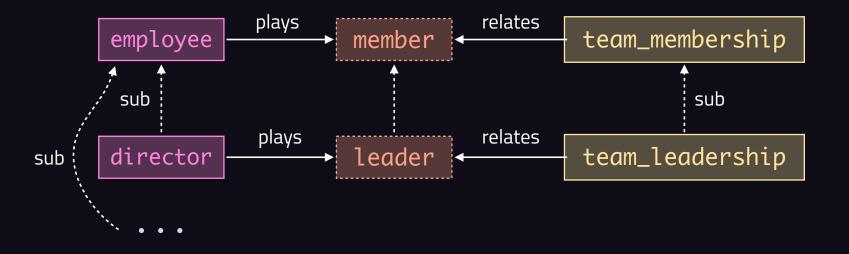




```
match
    $e isa employee;
    (team: $t, leader: $e) isa team_leadership;
fetch
    $e as leader: name;
    $t as team: team_name;
```

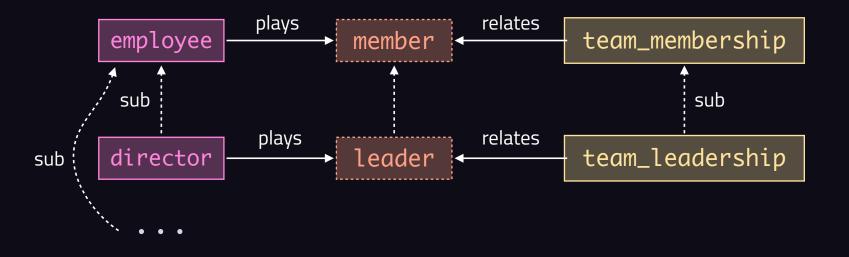
match clause, line 1

- States \$e is a employee object
- In particular, \$e could be a director object!





```
match
    $e isa employee;
    (team: $t, leader: $e) isa team_leadership;
fetch
    $e as leader: name;
    $t as team: team_name;
```

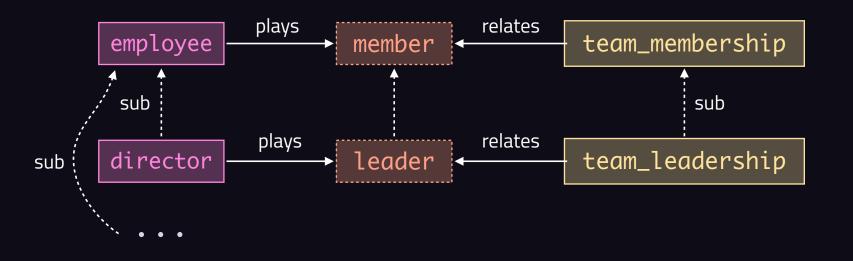


• match clause, line 1

- States \$e is a employee object
- In particular, \$e could be a director object!
- match clause, line 2
 - States a team_leadership exists with leader \$e
 - Can *infer* \$e is a director



```
match
    $e isa employee;
    (team: $t, leader: $e) isa team_leadership;
fetch
    $e as leader: name;
    $t as team: team_name;
```



match clause, line 1

- States \$e is a employee object
- In particular, \$e could be a director object!
- match clause, line 2
 - States a team_leadership exists with leader \$e
 - Can infer \$e is a director
- fetch clause:
 - The time we return tuples of employees \$e (with names) and teams \$t (with team_names)



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```

When clause contains a pattern stating the rule's assumptions



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```

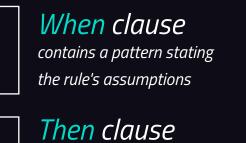


Then clause statement of data to be derived



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```

- when clause
 - States \$d is a director object
 - States \$d is a member in a team \$t







```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```

- when clause
 - States \$d is a director object
 - States \$d is a member in a team \$t
- then clause
 - States \$d is a leader of team \$t



Then clause statement of data to be derived



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```



Then clause statement of data to be derived

- when clause
 - States \$d is a director object
 - States \$d is a member in a team \$t
- then clause
 - States \$d is a leader of team \$t

In other words: *"directors are automatically designated as leaders in all teams they are members in."*



```
define rule director-team-members-are-leader: when {
    $d isa director;
    (team: $t, member: $d) isa team_membership;
} then {
    (team: $t, leader: $d) isa team_leadership;
};
```

When clause contains a pattern stating the rule's assumptions

Then clause statement of data to be derived

- when clause
 - States \$d is a director object
 - States \$d is a member in a team \$t
- then clause
 - States \$d is a leader of team \$t
- *Note*: same pattern-based QL used throughout!

In other words: *"directors are automatically designated as leaders in all teams they are members in."*







Summary

- **Patterns** in the PERA model:
 - express combined statement about type instances and dependencies
 - are fully composable and declarative
 - can be type-checked!



Summary

- **Patterns** in the PERA model:
 - express combined statement about type instances and dependencies
 - are fully composable and declarative
 - can be type-checked!
- Patterns underlie two *key functions* to the PERA model:
 - type-theoretic query language: TypeQL
 - rule-based Reasoning Engine



Summary

- **Patterns** in the PERA model:
 - express combined statement about type instances and dependencies
 - are fully composable and declarative
 - can be type-checked!
- Patterns underlie two *key functions* to the PERA model:
 - type-theoretic query language: TypeQL
 - rule-based Reasoning Engine

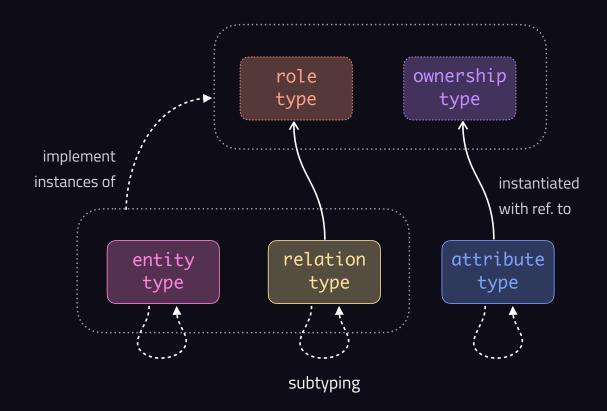




Lecture review: The PERA model

A fast evolving foundational model for modern databases

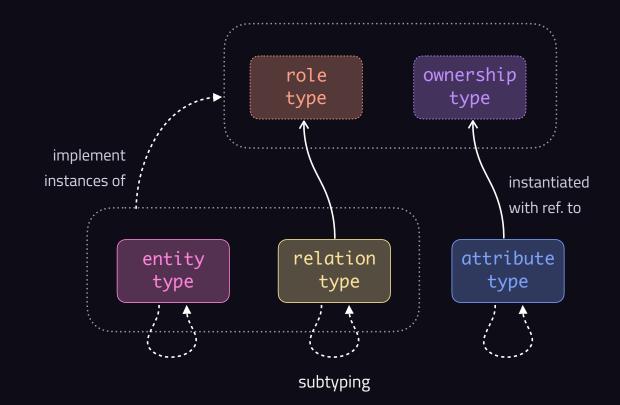




	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types



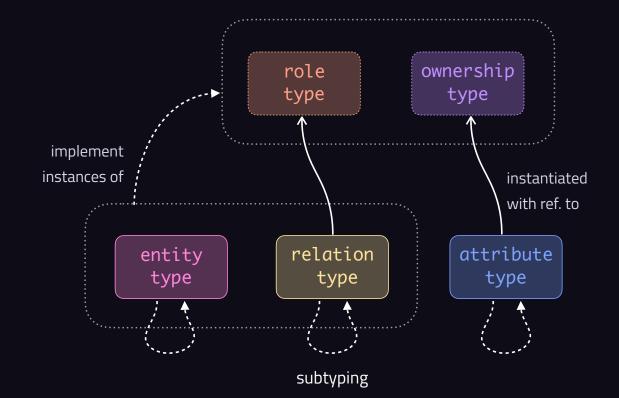
 We defined *concepts, instances,* and *concept dependencies* abstractly



	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types



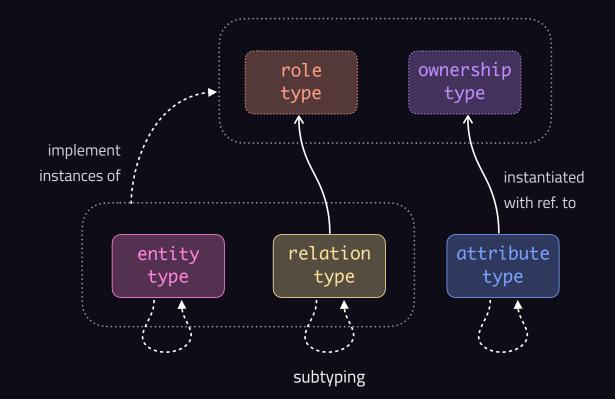
- We defined *concepts, instances,* and *concept dependencies* abstractly
- Used these simple conceptual principles to develop the PERA model



	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types



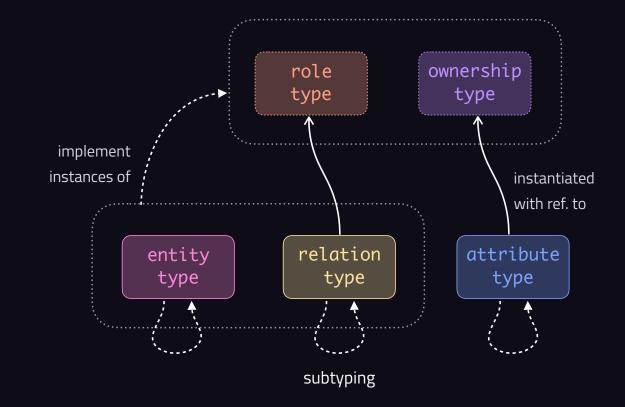
- We defined *concepts, instances,* and *concept dependencies* abstractly
- Used these simple conceptual principles to develop the PERA model
- Reverse-engineered concepts and dependencies of existing data models



	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types



- We defined *concepts, instances,* and *concept dependencies* abstractly
- Used these simple conceptual principles to develop the PERA model
- Reverse-engineered concepts and dependencies of existing data models

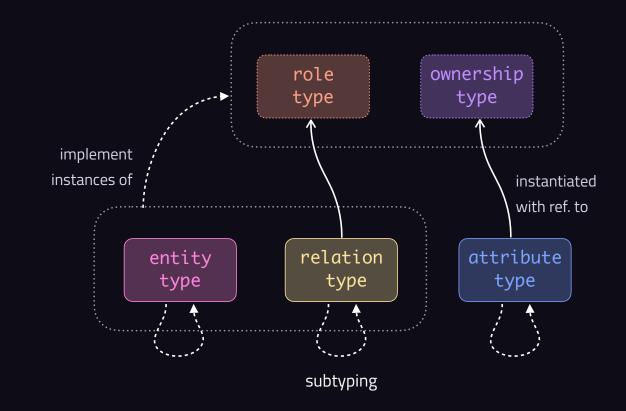


	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types

 In comparison, the PERA excels as a principled, modular, polymorphic, and types-first model



- We defined *concepts, instances,* and *concept dependencies* abstractly
- Used these simple conceptual principles to develop the PERA model
- Reverse-engineered concepts and dependencies of existing data models



	independent type	dependent type
object types	entity types	relation types
attribute types	(global constants)	attribute types

- In comparison, the PERA excels as a principled, modular, polymorphic, and types-first model
- Integrates type-theoretic querying and reasoning



Check out our previous lectures

Replay now available



TypeDB Lecture: Why We Need a Polymorphic Database TypeDB Fundamentals Lecture Series

0

Why We Need a Polymorphic Database





0



Watch at TypeDB.com/lectures



Vaticle TypeDB

Thank you!





More TypeDB Resources



TypeDB Learning Center typedb.com/learn



Download TypeDB typedb.com/deploy



TypeDB **Cloud** cloud.typedb.com



Vaticle TypeDB

Join us at typedb.com/discord